

MODELS FOR COMPUTING THE DIRECTIONAL
RADIATION OF SOUND FROM SOURCES
ON A RIGID CYLINDRICAL BAFFLE

Roland Ralph Johnson

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THESIS

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RADIATION OF SOUND FROM SOURCES
ON A RIGID CYLINDRICAL BAFFLE

by

Roland Ralph Johnson

December 1974

Thesis Advisor:

O.B. Wilson, Jr.

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Models for Computing the Directional
Radiation of Sound from Sources
on a Rigid Cylindrical Baffle

by

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Commander, United States Navy
B.S., United States Naval Academy, 1959

Submitted in partial fulfillment of the
requirements for the degree of

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ABSTRACT

The closed-form equations describing the acoustic radiation pattern for a source flush-mounted on a rigid cylindrical baffle are derived for three sonar transducer design configurations: two rectangular designs (Segment and Patch) and one circular configuration (Disk). The derivation includes both application and an extension of developments by previous theorists. A computer program based on the derived closed-form equations is included to permit design investigation of the three (3) configurations. Preliminary results of the program agree with previously obtained patterns by other investigators for the same source. The program, however, allows extension to new configurations.

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I. INTRODUCTION

Acoustic methods have for a long time proved useful for determining the position of objects submerged in the ocean and continue to be useful today, especially for monitoring the realistic testing of advanced underwater weapons (such as torpedoes) in the real ocean environment.

One method commonly used requires installation of a sound source on the underwater vehicle to be tracked. The source/vehicle is then tracked acoustically by hydrophones arrayed in a fixed position on the ocean bottom. The basic function is that of measuring the transit time of the sound wave from the source to different hydrophones. These transit times enable determination of distances and directions of arrival which in turn are triangulated to determine position, a series of which defines the vehicle's track.

As in most engineering problems, the requirements placed on an acoustic source used for tracking are often conflicting in nature, with the end result being an engineering compromise. For example, in order to achieve a broad pattern from a single element, the element's dimensions must be small relative to the wavelength of the sound transmitted. However, to obtain the desired sound pressure level, the element may have to be driven so hard that cavitation (an undesirable effect) results. For many practical reasons,

therefore, it is essential that the directional characteristics of a proposed transducer design be predicted prior to construction rather than measured afterwards. That is, a clear understanding of the relations between directivity and design constants is essential to properly design a transducer for a specific purpose.

Study of the geometry involved in tracking an underwater vehicle with ocean-floor mounted hydrophones (assuming that the hydrophones are not located at excessive depths) reveals that the slant range from the vehicle to the receivers is normally several orders of magnitude greater than the distance from the vehicle to the ocean floor. It is clear, then, that most of the acoustic energy from a source mounted on the underbody of a vehicle should be directed obliquely, with a relative minimum being transmitted directly down at the ocean floor. Consideration of a large slant range situation dictates that the directionality pattern extend almost to the horizontal, however, not to the degree that will result in surface reflections.

A feeling for the difficulty involved in practically achieving the radiation pattern previously described can be obtained by studying the P.M. Morse [Ref. 2] solution for a radially vibrating strip which extends indefinitely along a cylinder. For the physical dimensions of the baffle (torpedo) and the frequency (75KHz) involved in our case of interest, the Morse solution indicates the acoustic

radiation pattern will be highly directional and primarily will ensonify an area directly beneath the vehicle. That is, the combined effect of the cylindrical baffle and relatively high frequency focuses the acoustic radiation in a highly directional beam normal to the surface of the radiator. Obviously then, it can be anticipated that to achieve the obliquely oriented pattern desired, some method of countering this focusing must be incorporated in any proposed transducer design.

The intent of this report then is to describe procedures for computing one characteristic of a sound source used for underwater acoustic tracking - its acoustic radiation pattern. The approach will be mathematical in scope resulting in the development of a computer program which will calculate and plot the radiation pattern of a flush mounted radiator located on the wall of a cylindrical shape, such as that of a torpedo. The study will encompass three (3) proposed design configurations, described in the following section.

III. THEORY

A. BACKGROUND

The subject of sound radiation from vibrating objects is an old one and the journal literature is replete with papers on the theory. It appears that the particular problem at hand, radiation from a finite element on a rigid cylindrical baffle has not received much attention. Morse and Ingard [Ref. 3] treat the problem of radiation from line sources on a cylinder. Laird and Cohen [Ref. 1] developed a solution for the far field radiation from a rectangular patch on a rigid cylinder, which comes closest to representing the present problem. For this reason, it forms the basis for the model of rectangular sources and the beginning point for the model of a circular source. For the convenience of the reader, some of the results of Laird and Cohen are summarized below.

In their study, Laird and Cohen extended the theory of Morse [Ref. 2] to the case where the source is any separable function of the azimuthal and axial dimensions. In this thesis, their results will be applied to derive the equations for the "Patch" and "Segment" sources. In addition, an extension of their work to the general case of a non-separable source is included to describe the pattern of the "Disk" configuration.

The general approach developed by Laird and Cohen uses the cylindrical coordinate system shown in Figure 1. The method assumes that the source, which is mounted on a rigid cylinder, vibrates radially in such a manner that its velocity distribution may be represented as a separable function of the azimuth and axial dimensions. That is, the velocity distribution has the same functional form in the azimuthal direction independent of the axial dimension and vice versa. This is shown diagrammatically in Figure 2. The boundary condition at the surface of the cylinder/source can then be given by the following expression:

$$u_r|_{r=a} = U_0 e^{-i\omega t} \left(\sum_{m=0}^{\infty} a_m \cos m\phi \right) \left[\int_{-\infty}^{\infty} F(k_z) e^{ik_z z} dk_z \right] \quad (1)$$

where the Fourier cosine series represents the azimuthal dependence and the Fourier integral represents the axial dependence. The cosine series was arbitrarily chosen for mathematical convenience.

Having established the boundary condition, the general expression for a combination of outgoing cylindrical waves of even azimuthal dependence, given by

$$p(r, \phi, z) = e^{-i\omega t} \sum_{m=0}^{\infty} \cos m\phi \times \int_{-\infty}^{\infty} A_m(k_z) H_m^{(1)}(k_r r) e^{ik_z z} dk_z \quad (2)$$

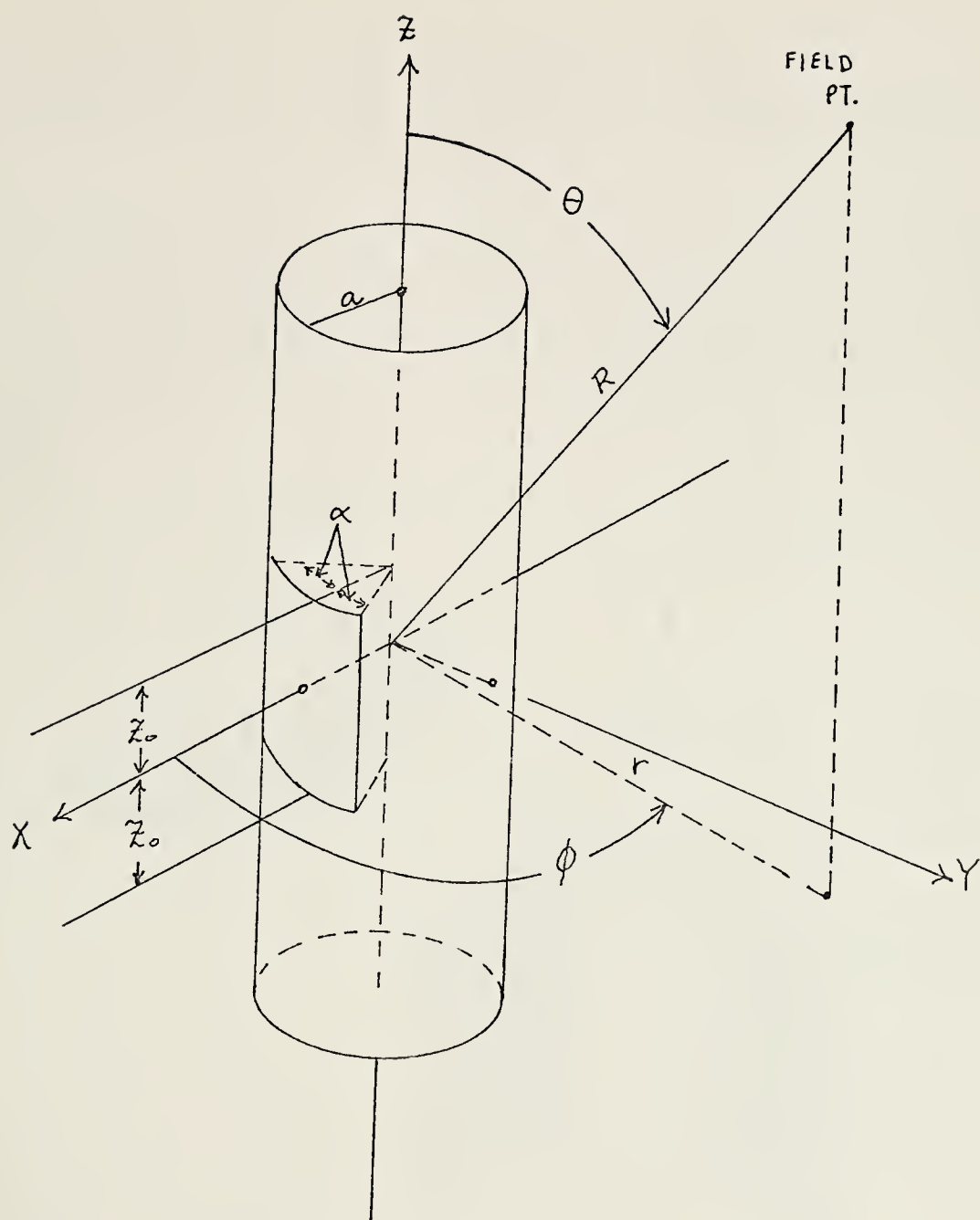


FIG. 1

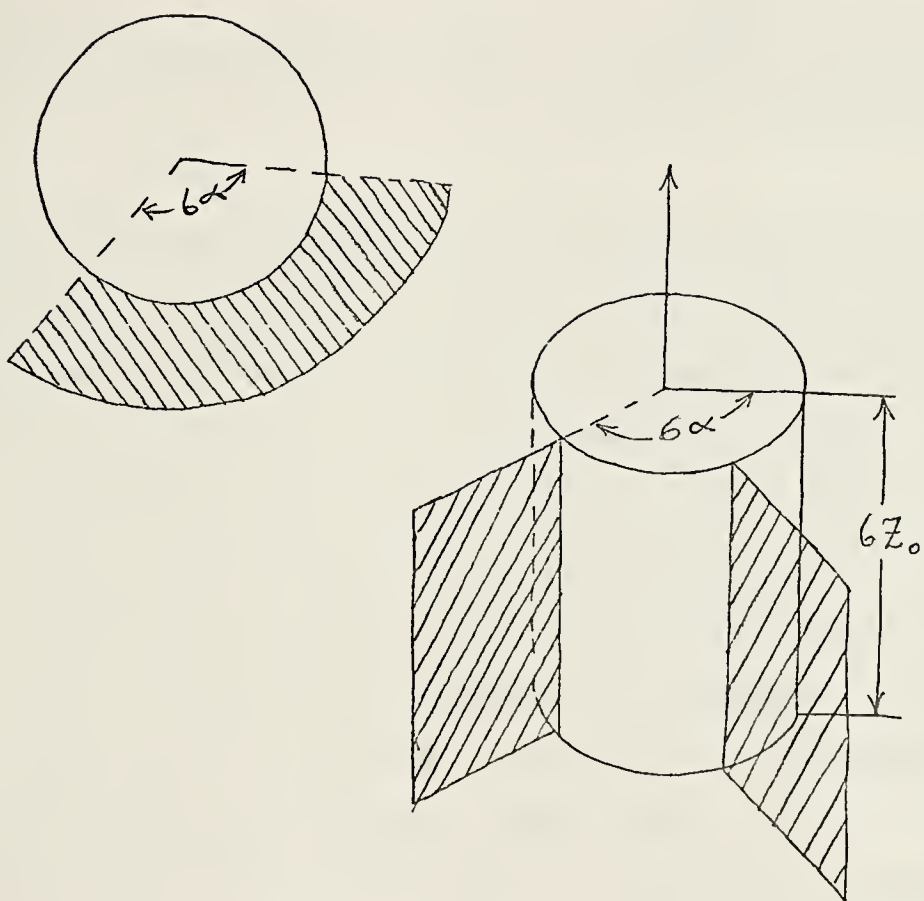


FIG. 2

is matched to the boundary condition at $r = a$ (the surface of the cylinder). Introduction of the far field approximation for the Hankel function, conversion to spherical coordinates, and the solution of a Fourier integral by the method of stationary phase result in the following general expression in spherical coordinates at a field point describing the radiation from a source on a rigid cylinder:

$$p(R, \theta, \phi) = 2\rho c U_0 \frac{e^{i(kR - \omega t)}}{R} \frac{F(k_z)}{\sin \theta} \times \sum_{m=0}^{\infty} \frac{a_m e^{-im\frac{\pi}{2}}}{H'_m(1) (k \sin \theta)} \cos m\phi \quad (3)$$

To consider a specific source using this method, one needs only to specify its location on the cylinder, physical dimensions and velocity distribution. Knowing the above, the Fourier coefficients, a_m , describing the azimuthal dependence and the Fourier transform, $F(k_z)$, describing the axial dependence, can be calculated. Substitution of the Fourier coefficients and the Fourier transform into Equation (3) results in an expression describing the radiation for the particular source considered. The frequency dependence is incorporated through the wave number, "k".

The derivation for the "Patch" configuration parallels the development for the case of the uniform rectangular source calculated by Laird and Cohen and illustrates use of Equation (3) for determining the radiation from a specific separable source.

B. PATCH CONFIGURATION

The "Patch" array (see Figure 3) is composed of nine equal-dimensioned elements (each of angular width 2α and height $2Z_0$) with the center element 180° out of phase with respect to the other elements.

Consideration of Figure 4 shows that the source motions of the patch cannot be described by separable, independent functions of the cylindrical coordinates ϕ and Z .

To avoid the complexities involved with a non-separable source, the entire array will be viewed as a simple rectangular source with uniform distribution (see Figure 5).

Likewise, the center element will be considered as a simple, uniformly excited rectangular source with dimensions 2α by $2Z_0$.

By subtracting twice the pattern function of the center element from that of the entire nine-element array, the desired result is achieved. This assumes the validity of the linear superposition principle.

The coefficients associated with the functions describing the source motion in azimuth are calculated using standard Fourier Series relationships. This results in:

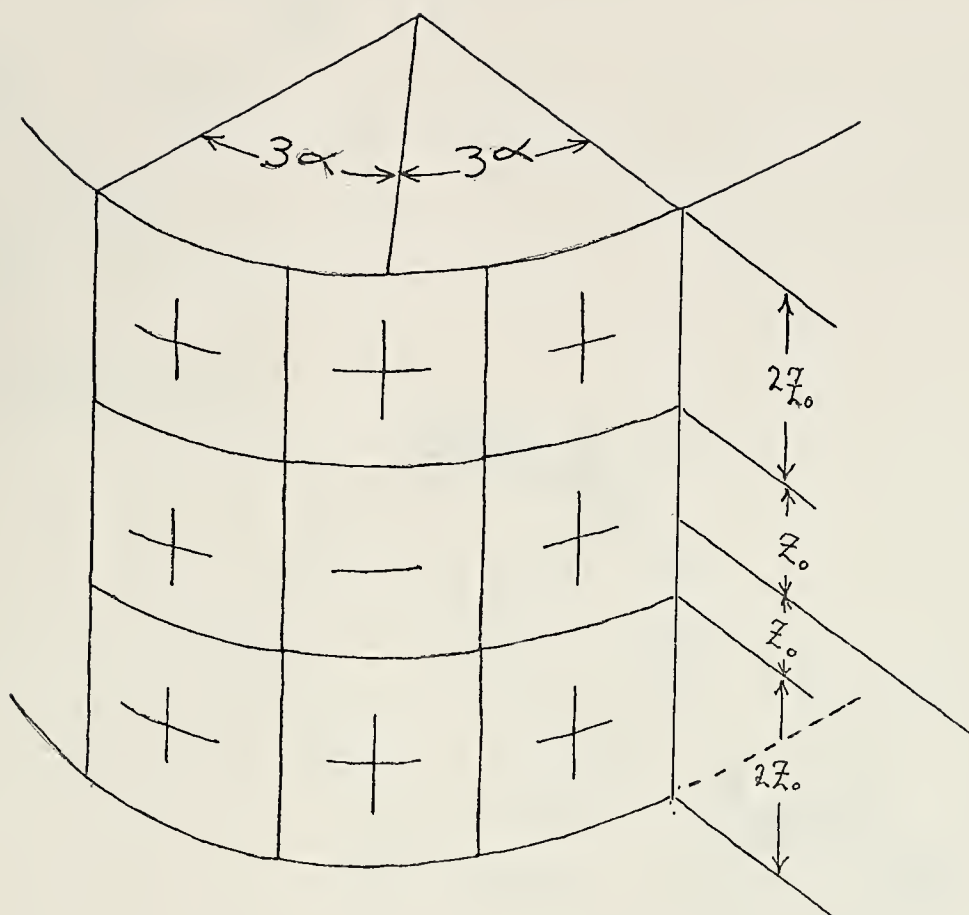
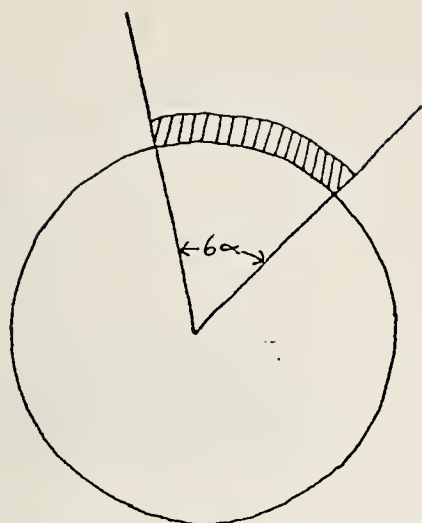
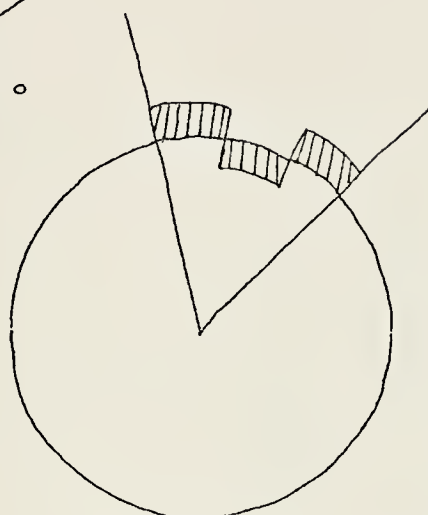


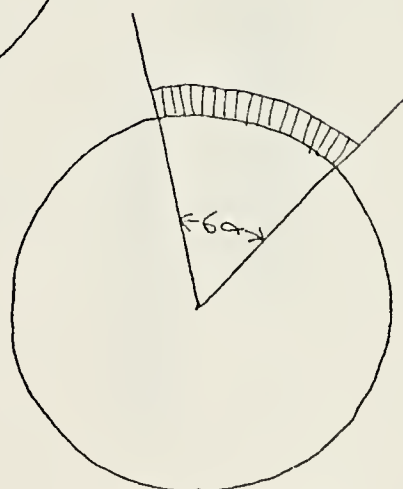
FIG. 3



$$-3Z_0 \leq Z \leq -Z_0$$



$$-Z_0 \leq Z \leq Z_0$$



$$Z_0 \leq Z \leq 3Z_0$$

FIG. 4

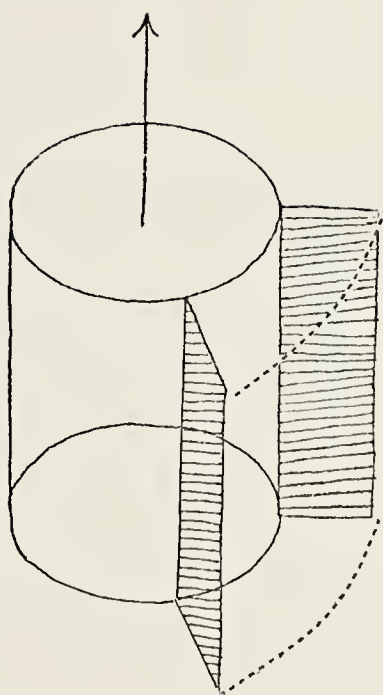
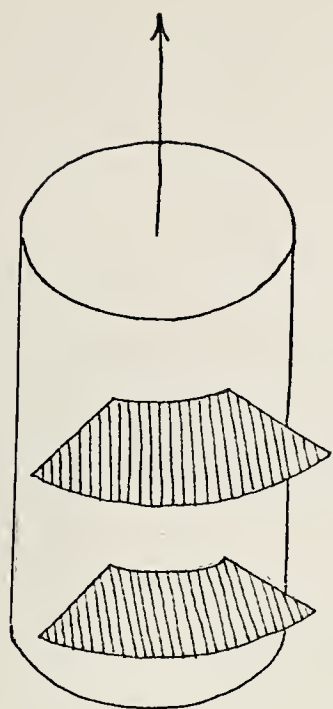


FIG. 5

For the center element of dimensions $(2\alpha, 2Z_0)$

$$a_0 = \frac{\alpha}{\pi} \quad a_m = \frac{2\sin m\alpha}{m\pi}$$

$$m = 1, 2, 3, \dots$$

For the entire array of dimensions $(6\alpha, 6Z_0)$

$$a_0 = \frac{3\alpha}{\pi} \quad a_m = \frac{2\sin 3m\alpha}{m\pi}$$

$$m = 1, 2, 3, \dots$$

Similarly the Fourier Transforms describing the axial dependence are

For the center element of dimensions $(2\alpha, 2Z_0)$

$$F(k_z) = \frac{\sin k_z Z_0}{\pi k_z}$$

For the entire array of dimensions $(6\alpha, 6Z_0)$

$$F(k_z) = \frac{\sin 3k_z Z_0}{\pi k_z}$$

Substitution into Equation (3) yields the following expression for the far-field pressure due to the radiation:

$$\begin{aligned} p(R, \theta, \phi) = & 2\rho c U_0 \frac{e^{i(kR - \omega t)}}{R} \left[\frac{\sin 3k_z Z_0}{\pi k_z} \left(\frac{3\alpha/\pi}{H'_0(1)} (k \sin \theta) \right. \right. \\ & + \sum_{m=1}^{\infty} \frac{2 \sin 3m\alpha / m\pi (e^{-im\pi/2})}{H'_m(1) (k \sin \theta)} \cos m\phi \\ & - \frac{2 \sin k_z Z_0}{\pi k_z} \left(\frac{\alpha/\pi}{H'_0(1)} (k \sin \theta) \right. \\ & \left. \left. + \sum_{m=1}^{\infty} \frac{2 \sin m\alpha / m\pi (e^{-im\pi/2})}{H'_m(1) (k \sin \theta)} \cos m\phi \right) \right] \quad (4) \end{aligned}$$

C. SEGMENT CONFIGURATION

The "Segment" array consists of elements of the same dimensions equally spaced about the circumference of the cylinder in the horizontal plane, that is, the plane perpendicular to the axis of the cylinder. This model permits specification of the amplitude and phase of motion for each element.

The following equation [Ref. 1] describes the far-field pressure in the horizontal plane for a single element of

dimensions 2α by $2Z_0$:

$$P(R, \frac{\pi}{2}, \phi) = \frac{2\rho c U_0 Z_0}{\pi} \frac{e^{i(kR - \omega t)}}{R} \times \left(\frac{\alpha/\pi}{H'_0(1)(ka)} \right. \\ \left. + \sum_{m=1}^{\infty} \frac{2\sin m\alpha/m\pi(e^{-im\frac{\pi}{2}})}{H'_m(1)(ka)} \cos m\phi \right) \quad (5)$$

In order to sum the contributions from all other elements which are disposed at uniform angles around the cylinder, it is necessary to transform the angle (ϕ) in Equation (5), so that it represents ϕ_i , the relative angle from the i th element to the field point, where the field point has spherical coordinates $(R, \frac{\pi}{2}, \beta)$ measured from the center of the cylinder.

Figure 6 illustrates the geometry of this for the i th element. The total number of elements was arbitrarily chosen to be 120. Thus, the spacing between adjacent elements is three (3) degrees for the computations for this design. The angular position of element number one (1) was arbitrarily chosen to be located at $\beta = 0$. The sum of the radiation from all elements, the pattern of each of which is given by Equation (5), results in:

$$P(R, \frac{\pi}{2}, \beta) = \frac{2\rho c U_0 Z_0}{\pi} \frac{e^{i(kR - \omega t)}}{R} \sum_{i=1}^{120} A_i (e^{i\gamma_i}) \left[\frac{\alpha/\pi}{H'_0(1)(ka)} \right. \\ \left. + \sum_{m=1}^{\infty} \frac{2\sin m\alpha/m\pi(e^{-im\frac{\pi}{2}})}{H'_m(1)(ka)} \cos m\phi_i \right] \quad (6)$$

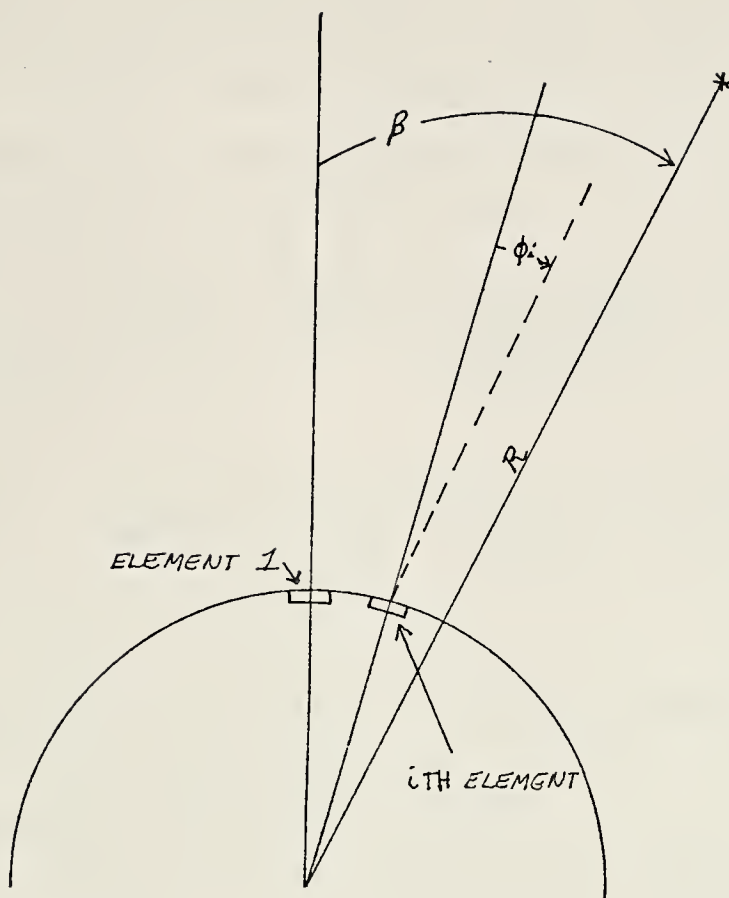


FIG. 6

where A_i is the relative amplitude of the i th element and γ_i is its relative phase and $\phi_i = [(i-1)3 + \beta]$.

In a similar manner, the following result is obtained for pressure as a function of the angle θ in a plane containing the axis of the cylinder:

$$P(R, \theta, \beta) = \frac{2\rho c U_o}{\pi} \frac{e^{i(kR - \omega t)}}{R} \frac{\sin(kZ_o \cos \theta)}{k \cos \theta \sin \theta} \times$$

$$\sum_{i=1}^{120} A_i e^{i\gamma_i} \left[\frac{\alpha/\pi}{H'_0(1) (k \sin \theta)} + \sum_{m=1}^{\infty} \frac{2 \sin m\alpha / m\pi (e^{-im\pi/2})}{H'_m(1) (k \sin \theta)} \cos m\phi_i \right] \quad (7)$$

where $\phi_i = [(i-1)3 + \beta]$, " i " = the i th element number.

D. CIRCULAR PISTON SOURCE (DISK)

The "Disk" array is composed of a central circular piston source which is surrounded by a concentric annular piston, with a 180 degree phase difference between their motions.

Since the motions of a circular piston located on the side of a cylinder cannot be described as separable functions of the cylinder coordinates, an extension of the methods described above must be made. Figure 7 shows (assuming a uniform velocity distribution) that although the functional form of the velocity distribution remains the same across the disk, the source is non-separable in that the axial limits are dependent on the azimuth dimension and vice versa.

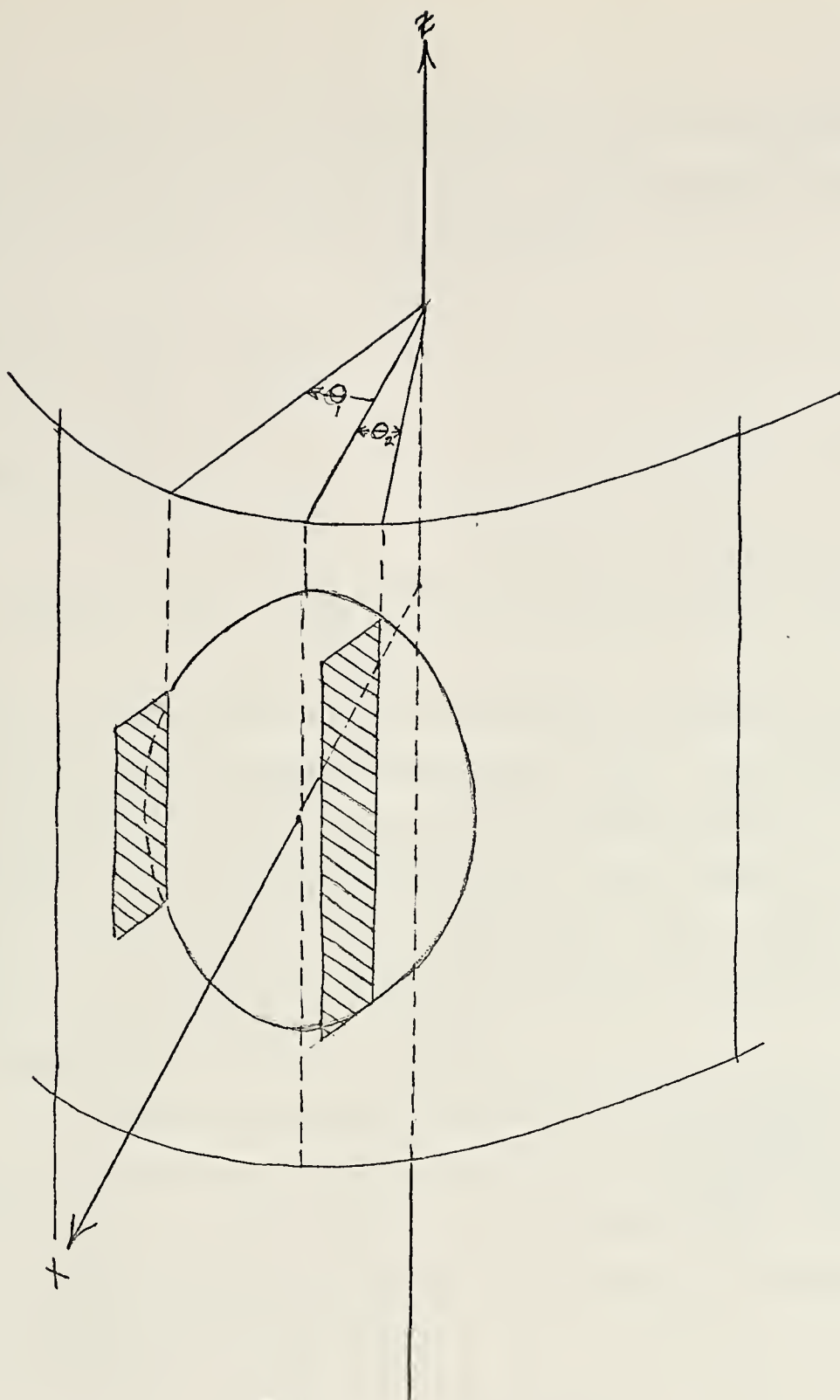


FIG. 7

Applying the boundary conditions for the circular piston using Equations (1) and (2) and the basic relation between particle velocity and pressure

$$u_r = - \frac{i}{\omega \rho} \frac{\partial p}{\partial r} \quad (8)$$

results in:

$$u_r|_{r=a} = -\frac{i}{\rho\omega} e^{-i\omega t} \sum_{m=0}^{\infty} (\cos m\phi) \int_{-\infty}^{+\infty} k_r A_m(k_z) H_m^{(1)}(k_r a) e^{ik_z Z} dk_z \quad (9)$$

Equating Equations (1) and (9) permits solution for $A_m(k_z)$ in terms of the Fourier coefficients, a_m . In the case of the separable source, the Fourier coefficients, a_m , are functions of the azimuth dimension of the source, ϕ . However, in the case of the non-separable source, they are also functions of the axial dimension (Z) and as such are expressible themselves as Fourier integrals.

To complete the general solution; having solved for $A_m(k_z)$, (in the separable case, $A_m(k_z) = \frac{i\rho\omega U_0 a_m F(k_z)}{k_r H_m^{(1)}(k_r a)}$) we substitute into Equation (2), the general equation for outgoing cylindrical waves of even azimuth dependence which yields the following:

$$p(r, \phi, Z) = e^{-i\omega t} \sum_{m=0}^{\infty} \cos m\phi \int_{-\infty}^{+\infty} \frac{i\rho\omega U_0 a_m}{k_r H_m^{(1)}(k_r a)} F(k_z) (H_m^{(1)}(k_r r) e^{ik_z Z} dk_z) \quad (10)$$

Introducing the far-field approximation for the Hankel function

$$H_m^{(1)}(k_r r) = \sqrt{\frac{2}{\pi k_r r}} e^{i k_r r} e^{-i(\frac{m\pi}{2} + \frac{\pi}{4})} \quad (11)$$

results in:

$$p(r, \phi, Z) = i\omega\rho U_0 \sqrt{\frac{2}{\pi r}} e^{-i\omega t} \sum_{m=0}^{\infty} a_m \cos m\phi e^{-i(m+\frac{1}{2})\frac{\pi}{2}} \\ \left(\int_{-\infty}^{+\infty} \frac{F(k_z) e^{i(k_r r + k_z Z)}}{k_r^{\frac{3}{2}} H_m^{(1)}(k_r a)} dk_z \right) \quad (12)$$

Converting to spherical coordinates, results in:

$$p(r, \theta, Z) = i\omega\rho U_0 \left(\frac{2}{\pi R \sin\theta}\right)^{\frac{1}{2}} e^{-i\omega t} \\ \times \sum_{m=0}^{\infty} a_m e^{-i(m+\frac{1}{2})\frac{\pi}{2}} \cos m\phi \quad (13) \\ \times \int_{-\infty}^{+\infty} \frac{F(k_z) \exp\{i[(k^2 - k_z^2)^{\frac{1}{2}} R \sin\theta + k_z R \cos\theta]\}}{(k^2 - k_z^2)^{\frac{3}{4}} H_m^{(1)}[(k^2 - k_z^2)^{\frac{1}{2}} a]} dk_z$$

Evaluating the Fourier Integral by the method of stationary phase gives as a final expression for the radiation:

$$p(R, \theta, \phi) = 2\rho c U_0 \frac{e^{i(kR - \omega t)}}{R} \frac{F(k_z)}{\sin\theta} \times \sum_{m=0}^{\infty} \frac{a_m e^{-im\frac{\pi}{2}}}{H_m^{(1)}(k a \sin\theta)} \cos m\phi \quad (14)$$

Returning to the non-separable disk, the boundary condition Equation (1), is again expressed as:

$$u_r|_{r=a} = U_o e^{-i\omega t} \left[\sum_{m=0}^{\infty} \cos m\phi a_m(z) \right] f(z) \quad (15)$$

where

$$f(z) = \int_{-\infty}^{\infty} F(k_z) e^{ik_z z} dk_z.$$

Since each term of the sum over "m" is multiplied by f(z), we may include f(z) in the sum. Thus,

$$u_r|_{r=a} = U_o e^{-i\omega t} \sum_{m=0}^{\infty} \cos m\phi a_m(z) f(z) \quad (16)$$

Now, let $g_m(z) = a_m(z)f(z)$.

Define

$$G_m(k_z) = F\{g_m(z)\} \text{ just as } F(k_z) = F\{f(z)\}$$

Then Equation (16) becomes:

$$u_r|_{r=a} = U_o e^{-i\omega t} \sum_{m=0}^{\infty} \cos m\phi \int_{-\infty}^{+\infty} G_m(k_z) e^{ik_z z} dk_z \quad (17)$$

Let $a_m = 1$ in Equation (1). Then Equation (17) is identical to Equation (1), which is from Laird and Cohen's development except that our $G_m(k_z)$ depends on "m" while the $F(k_z)$ in

Equation (3) does not. However, this still permits using Laird and Cohen's results; namely Equation (13) still applies with a_m in (13) set equal to one (1) and $G_m(k_z)$ replacing $F(k_z)$.

The parallel to Equation (14) then is:

$$p(R, \theta, \phi) = 2\rho c U_0 \frac{e^{i(kR - \omega t)}}{R \sin \theta} \sum_{m=0}^{\infty} \frac{G_m(k_z) e^{-im\frac{\pi}{2}}}{H_m^{(1)}(ka \sin \theta)} \cos m\phi \quad (18)$$

where we have set a_m equal to one (1) in Equation (14) and have replaced $F(k_z)$ by $G_m(k_z)$, but have included $G_m(k_z)$ within the summation over "m" because $G_m(k_z)$, unlike $F(k_z)$, depends on "m".

It remains, then, to evaluate $G_m(k_z)$ for the case at hand. The following was accomplished in collaboration with Steven R. Cohen [Ref. 5].

Noting that the equation of the disk on the cylinder is given by $z^2 + a^2 \phi^2 = z_0^2$ where $z_0 = a\alpha$, we solve for " ϕ " in terms of " z "

$$\phi = \pm \sqrt{\frac{z_0^2 - z^2}{a^2}} \quad .$$

Using this result, we can express the Fourier coefficients directly in terms of (z), the axial dimension:

$$\begin{aligned} a_0 &= \frac{\phi}{\pi} = \sqrt{\frac{z_0^2 - z^2}{a^2}} \left(\frac{1}{\pi} \right) \\ a_m &= 2 \sin \left(\frac{m \sqrt{\frac{z_0^2 - z^2}{a^2}}}{m\pi} \right) = \frac{2 \sin \left(\frac{m}{a} \sqrt{z_0^2 - z^2} \right)}{m\pi} \quad (19) \end{aligned}$$

Since $f(z) = 1$ (a constant)

$$\begin{aligned}
 G_m(k_z) &= F\{a_m(z)f(z)\} \\
 &= F\{a_m(z)\} = F\left\{\frac{2}{m\pi} \sin\left[\frac{m}{a}(z_o^2 - z^2)^{\frac{1}{2}}\right]\right\} \\
 &= \frac{2}{m\pi} \int_{-\infty}^{+\infty} \frac{e^{\frac{im}{a}\sqrt{z_o^2 - z^2}} - e^{-\frac{im}{a}\sqrt{z_o^2 - z^2}}}{2i} e^{-ik_z z} dz \quad (20)
 \end{aligned}$$

To evaluate this integral, we first let $k_z = \omega$, $z = t$ and $dz = dt$. Therefore

$$G_m(k_z) = \frac{1}{im\pi} \int_{-\infty}^{+\infty} (e^{\frac{im}{a}\sqrt{z_o^2 - t^2}} - e^{-\frac{im}{a}\sqrt{z_o^2 - t^2}}) e^{-i\omega t} dt \quad (21)$$

that is:

$$G_m(\omega) = F\left\{\frac{1}{m\pi i} e^{\frac{im}{a}\sqrt{z_o^2 - t^2}}\right\} - F\left\{\frac{1}{m\pi i} e^{-\frac{im}{a}\sqrt{z_o^2 - t^2}}\right\} \quad (22)$$

To evaluate the above Fourier transforms we will use the following standard Laplace transform relationships:

$$(1) \quad L\{J_0(a\sqrt{t^2 - b^2})\} = \frac{e^{-b\sqrt{s^2 - a^2}}}{\sqrt{s^2 + a^2}} \quad \text{for } t > b$$

$$(2) \quad L\{C(t, a)\} = C(s, a)$$

$$(3) \quad \int L\{C(t, a)\} da = \int C(s, a) da$$

Applying relationship (3) to (1)

$$\begin{aligned} L\{fJ_0(a\sqrt{t^2-b^2}) da\} &= \int \frac{e^{-b\sqrt{s^2+a^2}}}{\sqrt{s^2+a^2}} da \\ &= -\frac{1}{ab} e^{-b\sqrt{s^2+a^2}} \end{aligned} \quad (23)$$

Letting $b = \frac{im}{c}$, where "c" is chosen vice "a" to avoid confusion, i.e., $c = a$, and substituting into (23) yields

$$L\{fJ_0(a\sqrt{t^2+\frac{m^2}{c^2}}) da\} = -\frac{1}{a(\frac{im}{c})} e^{-\frac{im}{c}\sqrt{s^2+a^2}} \quad (24)$$

To evaluate the integral, $fJ_0(a\sqrt{t^2+\frac{m^2}{c^2}}) da$:

$$\text{Let } u = a\sqrt{t^2+\frac{m^2}{c^2}}. \text{ Therefore } du = \sqrt{t^2+\frac{m^2}{c^2}} da,$$

$$da = \frac{du}{\sqrt{t^2+\frac{m^2}{c^2}}}$$

$$\begin{aligned} fJ_0(a\sqrt{t^2+\frac{m^2}{c^2}}) da &= \frac{1}{\sqrt{t^2+\frac{m^2}{c^2}}} fJ_0(u) du \\ &= \frac{1}{\sqrt{t^2+\frac{m^2}{c^2}}} (2 \sum_{m=0}^{\infty} J_{2m+1}(u)) \\ &= \frac{2}{\sqrt{t^2+\frac{m^2}{c^2}}} [J_1(u) + J_3(u) + J_5(u) + \dots] \end{aligned} \quad (25)$$

Therefore Equation (24) becomes

$$\begin{aligned}
 & \mathcal{L}\left\{ \frac{2}{\sqrt{t^2 + \frac{m^2}{c^2}}} \left(J_1\left(a\sqrt{t^2 + \frac{m^2}{c^2}}\right) + J_3\left(a\sqrt{t^2 + \frac{m^2}{c^2}}\right) + J_5(\quad) + \dots \right) \right\} \\
 &= -\frac{c}{aim} e^{-\frac{im}{c}\sqrt{s^2 + a^2}} \quad (26)
 \end{aligned}$$

Substituting $s = j\omega$ to convert to the Fourier variable

$$\begin{aligned}
 & \mathcal{F}\left\{ \frac{2}{\sqrt{t^2 + \frac{m^2}{c^2}}} \left(J_1\left(a\sqrt{t^2 + \frac{m^2}{c^2}}\right) + J_3\left(a\sqrt{t^2 + \frac{m^2}{c^2}}\right) + \dots \right) \right\} \\
 &= -\frac{c}{aim} e^{-\frac{im}{c}\sqrt{a^2 - \omega^2}} \quad (27)
 \end{aligned}$$

which is of the form $\mathcal{F}\{f(t)\} = F(\omega)$.

Using the relationship $\mathcal{F}\{F(t)\} = 2\pi f(-\omega)$ with Equation (27) gives the result:

$$\begin{aligned}
 & \mathcal{F}\left\{ -\frac{c}{aim} e^{-\frac{im}{c}\sqrt{a^2 - t^2}} \right\} \\
 &= \frac{4\pi}{\sqrt{\omega^2 + \frac{m^2}{c^2}}} \left[J_1\left(a\sqrt{\omega^2 + \frac{m^2}{c^2}}\right) + J_3\left(a\sqrt{\omega^2 + \frac{m^2}{c^2}}\right) + J_5(\quad) + \dots \right] \quad (28)
 \end{aligned}$$

Taking the constant $(-\frac{c}{aim})$ outside the transform and dividing gives:

$$\begin{aligned}
& F\left\{e^{-\frac{im}{c}\sqrt{a^2-t^2}}\right\} \\
&= -\frac{aim}{c} \cdot \frac{4\pi}{\sqrt{\omega^2+\frac{m^2}{c^2}}} \left[J_1\left(a\sqrt{\omega^2+\frac{m^2}{c^2}}\right) + J_3\left(a\sqrt{\omega^2+\frac{m^2}{c^2}}\right) + J_5(\quad) + \dots \right]
\end{aligned} \tag{29}$$

which can be directly used to evaluate

$$F\left\{-\frac{1}{m\pi i} e^{-\frac{im}{a}\sqrt{z_o^2-z^2}}\right\}$$

where $m = m$, $c = a$, and $a = z_o$. Therefore,

$$\begin{aligned}
& F\left\{-\frac{1}{m\pi i} e^{-\frac{im}{a}\sqrt{z_o^2-z^2}}\right\} \\
&= -\frac{1}{m\pi i} \cdot \frac{miz_o}{a} \cdot \frac{4\pi}{\sqrt{\omega^2+\frac{m^2}{a^2}}} \left[J_1\left(z_o\sqrt{\omega^2+\frac{m^2}{a^2}}\right) + J_3(\quad) + \dots \right] \\
&= \frac{4z_o}{a\sqrt{\omega^2+\frac{m^2}{a^2}}} \left[J_1\left(z_o\sqrt{\omega^2+\frac{m^2}{a^2}}\right) + J_3(\quad) + J_5(\quad) + \dots \right]
\end{aligned} \tag{30}$$

A similar treatment letting $b = \frac{im}{c}$ permits the following:

$$\begin{aligned}
& F\left\{\frac{1}{m\pi i} e^{-\frac{im}{a}\sqrt{z_o^2-z^2}}\right\} \\
&= \frac{4z_o}{a\sqrt{\omega^2+\frac{m^2}{a^2}}} \left[J_1\left(z_o\sqrt{\omega^2+\frac{m^2}{a^2}}\right) + J_3(\quad) + J_5(\quad) + \dots \right]
\end{aligned} \tag{31}$$

Since

$$\begin{aligned}
 G_m(k_z) &= F\left\{\frac{2}{m\pi} \sin\left(\frac{m}{a}\sqrt{z_o^2 - z^2}\right)\right\} \\
 &= F\left\{\frac{1}{m\pi i} \cdot e^{\frac{im}{a}\sqrt{z_o^2 - z^2}}\right\} + F\left\{-\frac{1}{m\pi i} e^{-\frac{im}{a}\sqrt{z_o^2 - z^2}}\right\} \\
 G_m(k_z) &= \frac{8z_o}{a} \cdot \frac{1}{\sqrt{k_z^2 + \frac{m^2}{a^2}}} [J_1(z_o\sqrt{k_z^2 + \frac{m^2}{a^2}}) + J_3(z_o\sqrt{k_z^2 + \frac{m^2}{a^2}}) \\
 &\quad + J_5(\quad) + \dots] \\
 &= \frac{8z_o^2}{a} \left[\frac{J_1(z_o\sqrt{k_z^2 + \frac{m^2}{a^2}})}{z_o\sqrt{k_z^2 + \frac{m^2}{a^2}}} + \frac{J_3(z_o\sqrt{k_z^2 + \frac{m^2}{a^2}})}{z_o\sqrt{k_z^2 + \frac{m^2}{a^2}}} \right. \\
 &\quad \left. + \frac{J_5(\quad)}{(\quad)} + \dots \right] \tag{32}
 \end{aligned}$$

Substituting $G_m(k_z)$ into the general expression for the radiation, Equation (18), results in the following equation describing the radiation for a "disk" source on a cylindrical baffle:

$$\begin{aligned}
 p(R, \theta, \phi) &= \frac{16\rho c U_o z_o^2}{a} \frac{e^{i(kR - \omega t)}}{R \sin \theta} \sum_{m=0}^{\infty} \sum_{i=0}^{\infty} \frac{J_{2i+1}(z_o\sqrt{k_z^2 + \frac{m^2}{a^2}})}{z_o\sqrt{k_z^2 + \frac{m^2}{a^2}}} \\
 &\quad \times \frac{e^{-im\frac{\pi}{2}}}{H'_m(1)(k \sin \theta)} \cos m\phi \tag{33}
 \end{aligned}$$

The pattern for the "Disk" design is achieved by subtracting twice the pattern of the inner circular piston source from that of a circular piston source having a diameter equal to that of the outer concentric annular piston.

III. COMPUTER MODELS

A. GENERAL DESCRIPTION

Based on the closed-form equations derived in the previous section, a computer program was written to permit rapid calculation and plotting of the directivity patterns for the designs of interest. A complete listing of the program developed is included as Appendix A. A brief description of each of the major subroutines which comprise the program is included as Appendix B.

Through the use of the program, the parameters which effect the radiation pattern of a particular source can be varied and their effect on the radiation pattern noted. In this manner, a design for a particular configuration can be achieved.

The parameters affecting the radiation pattern are changed through the use of "data inputs" to the program. The data inputs permit the following: (1) changing the physical dimensions of each of the sources, (2) changing the frequency at which the source is operated, (3) changing the radius of the cylindrical baffle on which the source is mounted, and (4) selecting the plane in which the directivity pattern is desired. In addition, for the use of the "Segment" design, the program inputs permit specifying the amplitude and phase shading of each of the individual

elements of the array. However, in this case only the resulting beam pattern in the horizontal plane can be plotted.

Another input which was added to increase the flexibility of operation of the program is the "summations limit". As can be noted from the equations derived in the previous section, all of the radiation pattern equations include an infinite series summation. Although this limit remains an input variable to the program, judicious use of this input is recommended if correct results are to be obtained. This matter will be discussed further in the "Results" section of this thesis.

Program outputs are both tabular and graphical in character and can be summarized as follows: (1) The computed values of the real and imaginary parts of the complex pressure for one (1) degree bearing increments expressed in dynes per square meter, (2) The magnitude of the complex pressure for one (1) degree bearing increments expressed in dynes per square meter, (3) The magnitude of the complex pressure for one (1) degree bearing increments expressed in decibels referenced to one microbar, (4) A polar plot of the magnitude of the complex pressure normalized to the largest value of the complex pressure, (5) A polar plot of the sound pressure level in decibels, normalized to the level of the largest lobe, using a scale length of 50 dB.

B. DESCRIPTION OF COMPUTER PROGRAM OPERATING PROCEDURES

A sample input data deck is included as Appendix C to illustrate these written instructions.

With the exception of the amplitude and phase shading portion of the "Segment" design, the input data decks required to obtain directionality patterns for each of the three (3) configurations are identical. The first data card indicates the configuration for which a beam pattern is desired. This is accomplished by typing the name of the configuration (PATCH, DISK, OR SEGEMENT) as shown on the first data card commencing in column number one (1). The second data card indicates the number of summations desired and the physical characteristics of an element of the particular design for which the pattern is being calculated. The number of summations desired is typed in columns one (1) and two (2), [FORMAT I2], one-half the height (z_0) of a single element measured in meters is entered in columns 11-20 [FORMAT F10.5] (in the case of the DISK the outer radius measured in meters), one-half the angular width of a single element (α) measured in radians is entered in columns 21-30 [FORMAT F10.5] (in the case of the DISK - the inner radius measured in meters), the radius of the cylinder measured in meters in columns 31-40, and frequency in KHz (i.e. for 75 KHz type "75.") in columns 41-50 [FORMAT F10.5]. The third and final data card indicates the plane in which

a pattern is desired and the angle which is to be held constant for the calculation. By reference to Figure 1, one can see that by setting ϕ equal to a constant and summing θ , a pattern in a plane containing the axis of the cylinder is achieved. Likewise, by setting θ equal to a constant and summing ϕ , a pattern for a plane orthogonal to the axis of the cylinder is obtained. In this manner, various planes for a particular source and three (3) dimensional aspects of the pattern can be perceived and investigated. Indication of the angle which it is desired to vary is indicated by typing a "1" (Theta varying) or a "2" (Phi varying) in columns 1-2 [FORMAT I2]. The angle held constant is indicated by typing the angle (in degrees) in columns 11-20 [FORMAT F10.5].

To obtain a pattern in the horizontal plane for amplitude and phase shading for the "Segment" design, enter a "1" or "2" in column "2" [FORMAT I2] of the fourth card of the Segment Data Deck. On the subsequent card (the fifth card of the data deck) enter the total number of elements to be shaded using columns 1-3 [FORMAT I3] (i.e. if 24 elements are to be shaded, type "24" in columns 2 and 3). Following this card, a separate card for each of the elements requiring shading is entered. In columns 1-3 the element number to be shaded is entered [FORMAT I3], in columns 11-20 the amplitude of the shading is entered, [FORMAT F10.5] in columns 21-30 the desired phase shading is entered [FORMAT F10.5] as an angle.

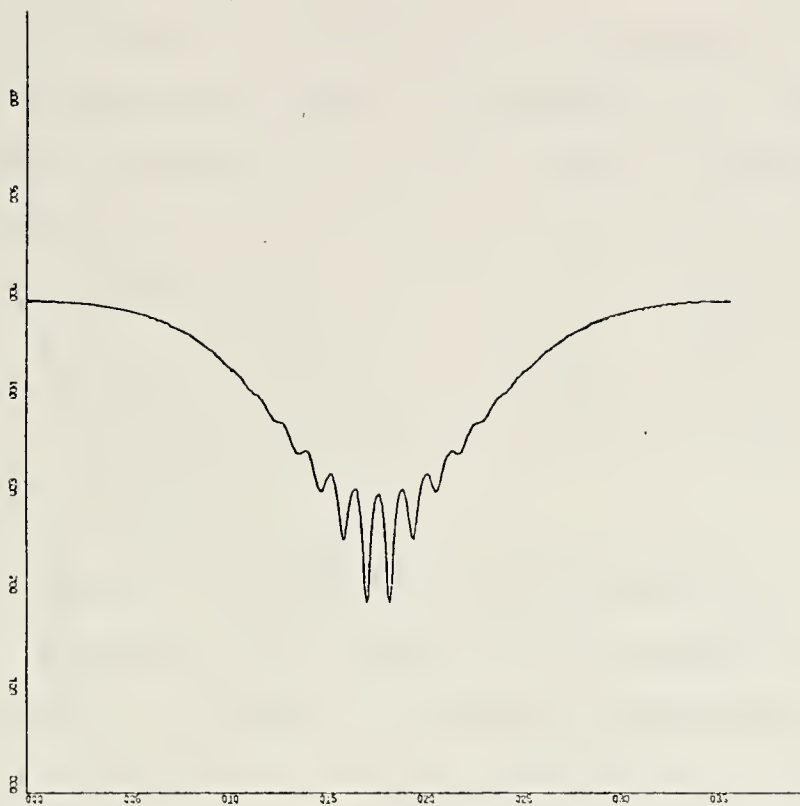
IV. RESULTS

A. PATTERN FOR UNIFORMLY EXCITED RECTANGULAR PATCH

Figure 8 shows the horizontal directivity pattern calculated for a single element ($\alpha = 3.7^\circ$, $ka = 14$) using the "Segment" subroutine. The pattern was calculated and plotted in rectangular coordinates to permit a direct comparison to a similar pattern plotted by Laird and Cohen [Ref. 1] using the same input variables. Comparison of the two patterns shows they are identical. This result verifies that the basic coding of the program is correct.

B. EFFECT OF VARYING THE NUMBER OF SUMMATIONS

As noted previously, judicious use of the summing limit is required if accurate results are to be obtained. Runs for the same configuration were made with $N = 5, 10, 15, 20, 25, 30$, and 35 . Little to no observable change was noted in patterns for the runs with " N " greater than twenty (20). However, for runs with " N " less than twenty (20), the pattern varied considerably for each run. Experience with the program indicates that about 20-25 terms of the infinite series (which appears in the pattern function of all designs considered) must be calculated before the divergence of the Hankel derivations in the denominator cause the solution to converge. This conclusion concurs with that arrived at by Laird and Cohen in their original development.



X-SCALE=5.00E+01 UNITS INCH.
Y-SCALE=1.00E+01 UNITS INCH.
PLOT OF RAD IN DB

FIG. 8

As indicated by the comments in the BESJ SUBROUTINE listing, a maximum of twenty summations should be calculated if the value of the entering argument is less than fifteen (15).

To meet both the previously mentioned requirements, it is recommended that the summing limit always be set equal to twenty (20) for any final computations of a proposed design. The ability to change the number of summations has been included to permit a rapid rough first-cut. The execution time for the computer solution varies from 5-20 minutes dependent on the number of summations and the input parameters.

C. FREQUENCY DEPENDENCE OF THE SOLUTION

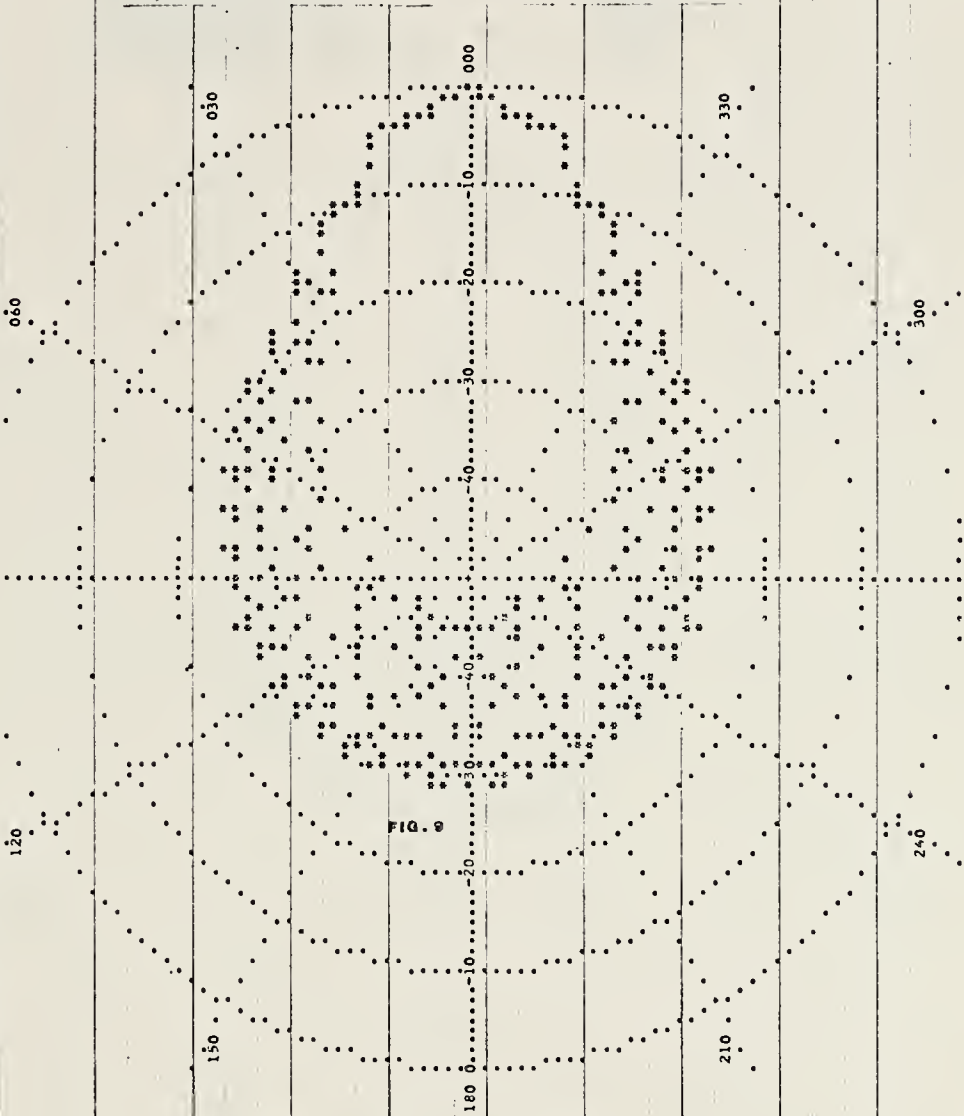
Figures 9, 10, 11 and 12 are included as examples of the manner in which the frequency dependence of the patterns can be studied. All input variables were held constant and the frequency was varied to obtain these patterns. The important design capability provided by this feature is the ability to predict the effect of the frequency bandwidth of a proposed design on the acoustic radiation pattern.

THIS RUN IS FOR A TRANSDUCER OF THE SEGMENT TYPE.

NUMBER OF SUMMATIONS	20
TRANSDUCER HEIGHT (METERS)	.20000E-01
TRANSDUCER WIDTH (RADIAN)	.18748E-01
RADIUS OF CYLINDER (METERS)	.26670E 00
FREQUENCY (KHZ)	.65090E 02
TYPE OF PLOT (1: THETA VARYING, 2: PHI VARYING)	2
PLANE ANGLE HELD CONSTANT FOR PLOT	.90000E 02

NORMALIZING FACTOR= 0.50000E 02

NORMALIZED DECIBEL (DB) PATTERN

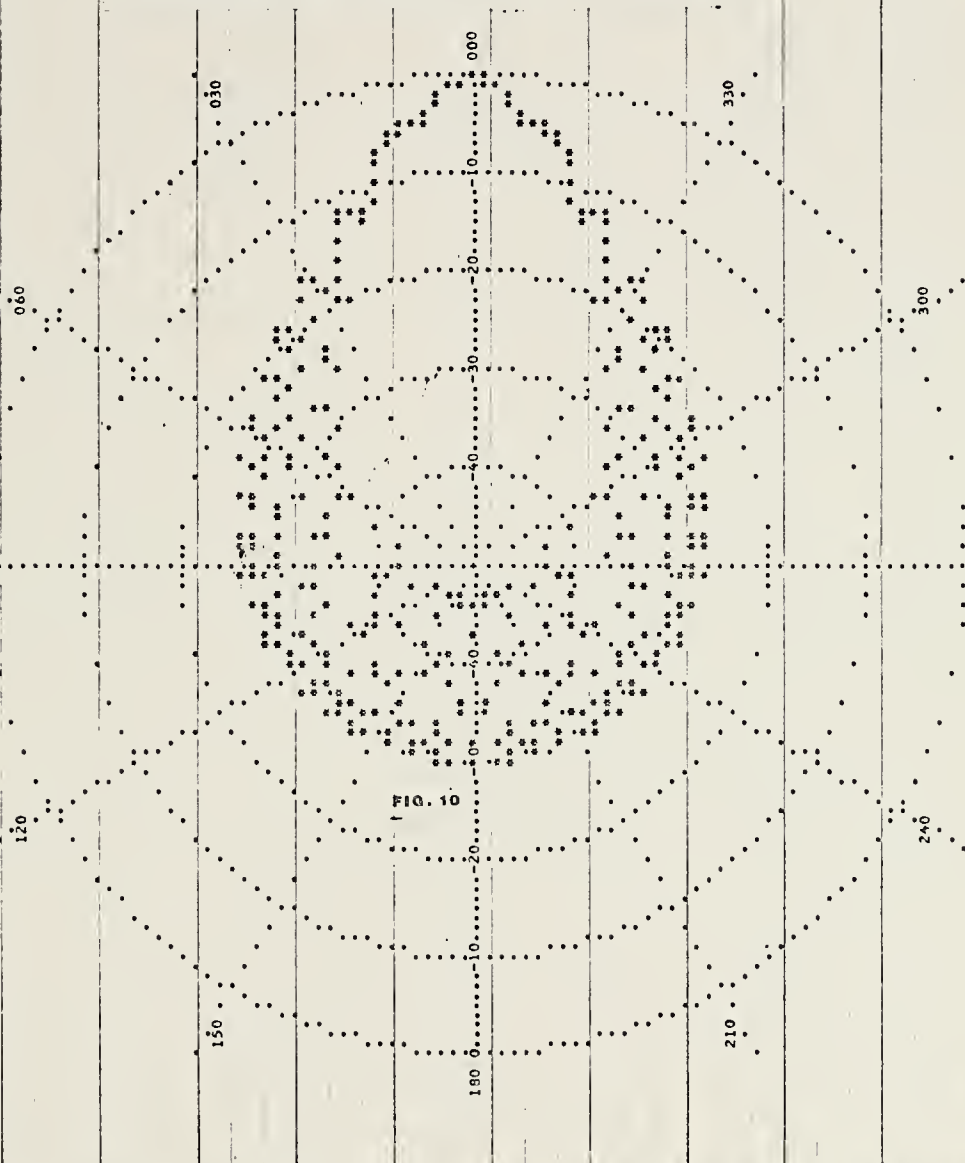


THIS RUN IS FOR A TRANSDUCER OF THE SEGMENT TYPE.

NUMBER OF SUMMATIONS	20
TRANSDUCER HEIGHT (METERS)	.20000E-01
TRANSDUCER WIDTH (RADIAN)	.18748E-01
RADIUS OF CYLINDER (METERS)	.26670E 00
FREQUENCY (KHZ)	.75000E 02
TYPE OF PLOT (1: THETA VARYING, 2: PHI VARYING)	2
PLANE ANGLE HELD CONSTANT FOR PLOT	.90000E 02

NORMALIZING FACTOR= 0.50000E 02

NORMALIZED DECIBEL (DB) PATTERN

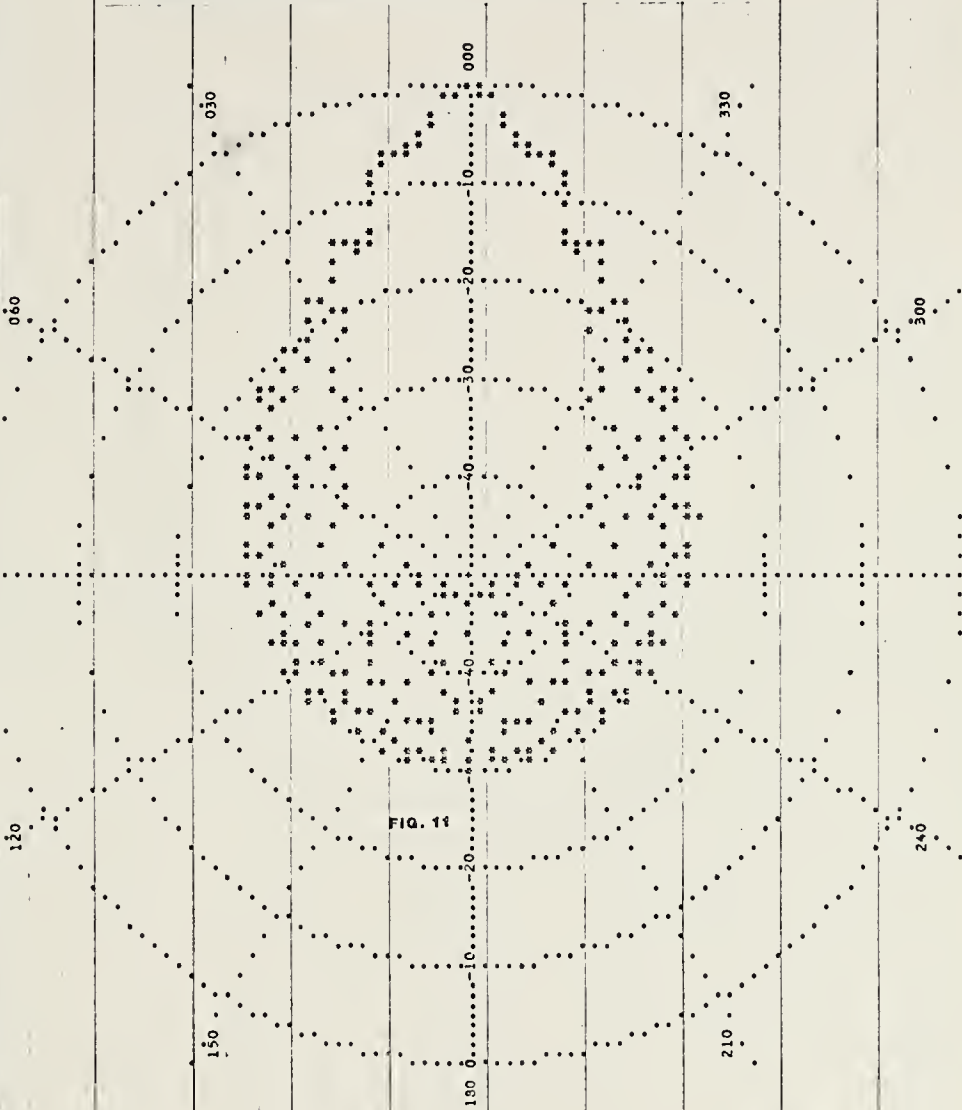


THIS RUN IS FOR A TRANSDUCER OF THE SEGMENT TYPE.

NUMBER OF SUMMATIONS	20
TRANSDUCER HEIGHT (METERS)	.20000E-01
TRANSDUCER WIDTH (RADIAN)	.18748E-01
RADIUS OF CYLINDER (METERS)	.26670E 00
FREQUENCY (KHZ)	.85000E 02
TYPE OF PLOT (1: THETA VARYING, 2: PHI VARYING)	2
PLANE ANGLE HELD CONSTANT FOR PLOT	.90000E 02

NORMALIZING FACTOR= 0.50000E 02

NORMALIZED DECIBEL (DB) PATTERN



FACTOR= 0.50000E 02

NORMALIZING

NORMALIZED DECIBEL(08) PATTERN

THIS RUN IS FOR A TRANSDUCER OF THE SEGMENT TYPE.

NUMBER OF SUMMATIONS 20
 TRANSDUCER HEIGHT (METERS) .20000E-01
 TRANSDUCER WIDTH (RADIAN) .18748E-01
 RADIUS OF CYLINDER (METERS) .26670E 00
 FREQUENCY (KHZ) .25000E 02
 TYPE OF PLOT (1: THETA VARYING, 2: PHI VARYING) 2
 PLANE ANGLE HELD CONSTANT FOR PLOT .90000E 02

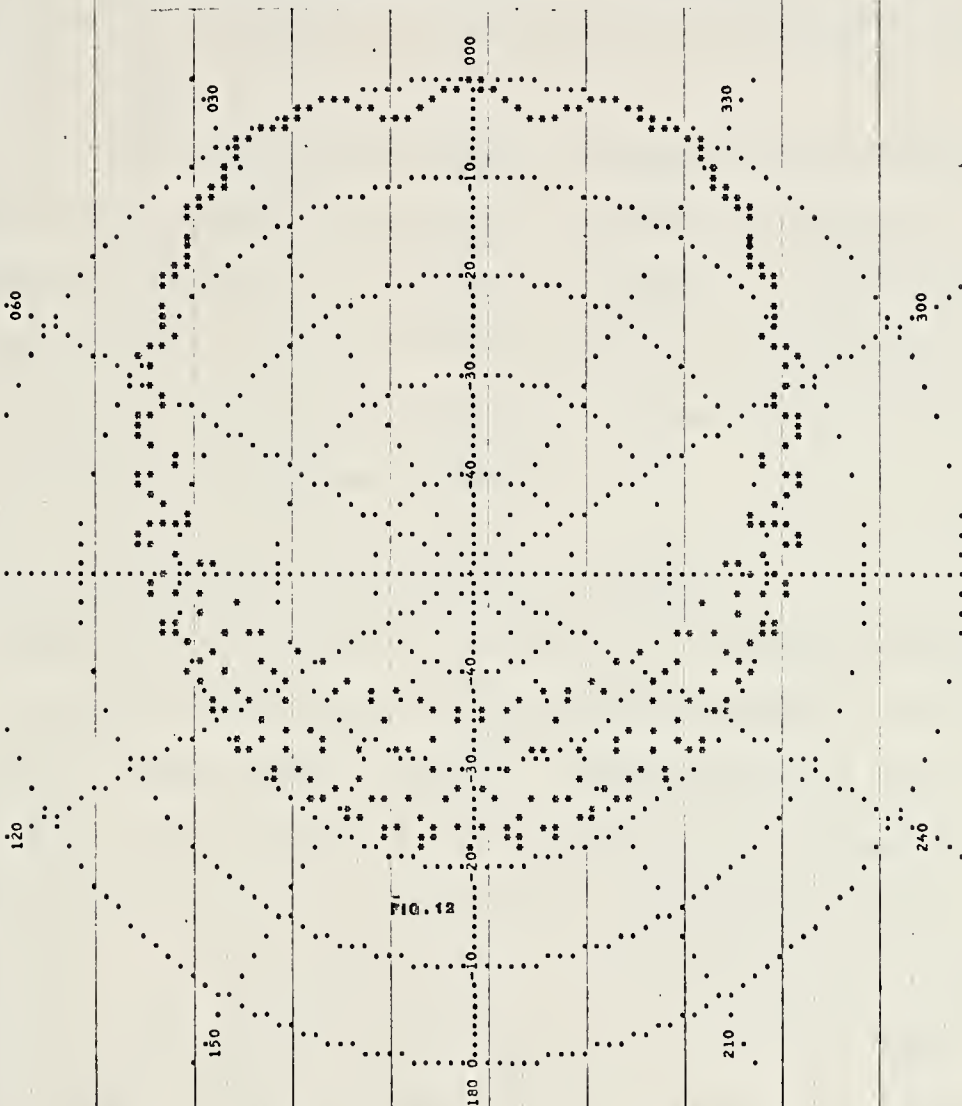


FIG. 12

V. CONCLUSIONS AND RECOMMENDATIONS

Computer models which permit the computation of the sound radiation pattern for three (3) different source configurations mounted on a rigid cylindrical baffle have been developed.

The computer solutions agree favorably with previous mathematical results obtained by earlier investigators. Although empirical data are not available for confirmation of the patterns, it is considered that good agreement would result due to the manner in which the curvature of both the source and baffle were treated.

A. RECOMMENDATIONS FOR FUTURE DEVELOPMENT

Although the program as it exists is a useful design tool, several future modifications would enhance its capabilities. These items include: incorporation of amplitude and phase shading in the axial plane for the "Segment" design and incorporation of a 3-dimensional plotting package for all designs. Another improvement envisaged would be the linkage of this program with available parameter optimization programs [Ref. 6 and 7] using response surface methodology to determine specific input parameters for a desired pattern.

APPENDIX A

```

1 DATA ASEG,APAT,ADISK/'SEGE','PATC','DISK'//
2 READ(5,5,END=4) A
3 WRITE(6,6)
4 IF(A.EQ.ASEG) WRITE(6,8)
5 IF(A.EQ.ASEG) CALL SEG
6 IF(A.EQ.APAT) WRITE(6,9)
7 IF(A.EQ.APAT) CALL PATCH
8 IF(A.EQ.ADISK) WRITE(6,10)
9 IF(A.EQ.ADISK) CALL DISK
10 IF((A.EQ.ASEG).OR.(A.EQ.APAT).OR.(A.EQ.ADISK)) GO TO 1
11 WRITE(6,7)
12 STOP
13
14 FORMAT(1A4)
15 FORMAT(1H1)
16 ***FIRST DATA CARD MUST BE TYPE OF TRANSDUCER ***
17 FORMAT(10X,'THIS RUN IS FOR A TRANSDUCER OF THE SEGMENT TYPE.////')
18 FORMAT(40X,'THIS RUN IS FOR A TRANSDUCER OF THE PATCH TYPE.////')
19 FORMAT(40X,'THIS RUN IS FOR A TRANSDUCER OF THE DISK TYPE.////')
20 END
21
22 .....
23 SUBROUTINE BESJ
24
25 PURPOSE
26 COMPUTE THE J BESSEL FUNCTION FOR A GIVEN ARGUMENT AND ORDER
27
28 USAGE
29 CALL BESJ(X,N,BJ,D,IER)
30
31 DESCRIPTION OF PARAMETERS
32 X -THE ARGUMENT OF THE J BESSEL FUNCTION DESIRED
33 N -THE ORDER OF THE J BESSEL FUNCTION DESIRED
34 BJ -THE RESULTANT J BESSEL FUNCTION
35 D -REQUIRED ACCURACY
36 IER--RESULTANT ERROR CODE WHERE
37 IER=0 NO ERROR
38 IER=1 N IS NEGATIVE
39 IER=2 X IS NEGATIVE OR ZERO
40 IER=3 REQUIRED ACCURACY NOT OBTAINED
41 IER=4 RANGE OF N COMPARED TO X NOT CORRECT (SEE REMARKS)
42
43 REMARKS
44 N MUST BE GREATER THAN OR EQUAL TO ZERO, BUT IT MUST BE
45 LESS THAN
46 20+10*X-X** 2/3 FOR X LESS THAN OR EQUAL TO 15
47 90+X/2 FOR X GREATER THAN 15
48
49 CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

```



```

SUBROUTINES AND FUNCTION SUBPROGRAMS REQUIRED
NONE
METHOD
RECCURENCE RELATION TECHNIQUE DESCRIBED BY H. GOLDSTEIN AND
R.M. THALER, RECURRENCE TECHNIQUES FOR THE CALCULATION OF
BESSEL FUNCTIONS, M.T.A.C., V.13, PP.102-108 AND I.A. STEGUN
AND M. ABRAMOWITZ, GENERATION OF BESSEL FUNCTIONS ON HIGH
SPEED COMPUTERS, M.T.A.C., V.11, 1957, PP.255-257
.....
SUBROUTINE BESJ (X,N,BJ,D,IER)
BJ = .0
IF (N) 1,2,2
IER = 1
1 RETURN
2 IF (X) 3,3,4
3 IER = 2
4 RETURN
5 IF (X-15.) 5,5,6
NTEST = 20.+10.*X-X**2/3
GO TO 7
6 NTEST = 90.+X/2.
7 IF (N-NTEST) 9,8,8
8 IER = 4
9 RETURN
IER = 0
10 IER = N+1
BPREV = .0
COMPUTE STARTING VALUE OF M
IF (X-5.) 10,11,11
10 MA = X+6.
GO TO 12
11 MA = 1.4*X+60./X
12 MB = N+IFIX(X)/4+2
MZERO = MAX0(MA,MB)
SET UPPER LIMIT OF M
MMAX = NTEST
DO 21 M=MZERO,MMAX,3
21 SET F(M),F(M-1)

```



```

C
77 FM1 = 1.0E-28
78 FM = .0
79 ALPHA = .0
80 IF (M-(M/2)*2) 14,13,14
81 JT = -1
82 GO TO 15
83 JT = 1
84 M2 = M-2
85
86
87 DO 18 K=1,M2
88 MK = M-K
89 BMK = 2.*FLOAT(MK)*FM1/X-FM
90 FM1 = FM
91 IF (MK-N-1) 17,16,17
92 BJ = BMK
93 JT = -JT
94 S = 1+JT
95 ALPHA = ALPHA+BMK*S
96
97 BMK = 2.*FM1/X-FM
98 IF (N) 20,19,20
99 BJ = BMK
100 ALPHA = ALPHA+BMK
101 BJ = BJ/ALPHA
102 IF (ABS(BJ-BPREV)-ABS(D*BJ)) 22,22,21
103 BPREV = BJ
104
105 IER = 3
106 RETURN
107 END
108 .....
109
110 SUBROUTINE BESY
111
112 PURPOSE
113 COMPUTE THE Y BESSEL FUNCTION FOR A GIVEN ARGUMENT AND ORDER
114
115 USAGE
116 CALL BESY(X,N,BY,IER)
117
118 DESCRIPTION OF PARAMETERS
119 X -THE ARGUMENT OF THE Y BESSEL FUNCTION DESIRED
120 N -THE ORDER OF THE Y BESSEL FUNCTION
121 BY -THE RESULTANT Y BESSEL FUNCTION
122 IER-RESULTANT ERROR CODE WHERE
123 IER=0 NO ERROR

```




```

65 B = A*T1
66 C = X-.7853982
67 Y0 = A*P0*SIN(C)+B*Q0*COS(C)
68 Y1 = -A*P1*COS(C)+B*Q1*SIN(C)
69 GO TO 9
70
71 . COMPUTE YO AND YI FOR X LESS THAN OR EQUAL TO 4
72
73
74
75
76
77
78
79
80 DO 7 L=1,15
81 IF (L-1).5.6,5
82 SUM = SUM+1./FLOAT(L-1)
83 FL = L
84 TS = T-SUM
85 TERM = (TERM*(-X2)/FL**2)*(1.-1./(FL*TS))
86 Y0 = Y0+TERM
87
88 TERM = XX*(T-.5)
89 SUM = 0
90 Y1 = TERM
91
92 DO 8 L=2,16
93 SUM = SUM+1./FLOAT(L-1)
94 FL = L
95 FL1 = L-1
96 TS = T-SUM
97 TERM = (TERM*(-X2)/(FL1*FL))*(TS-.5/FL)/(TS+.5/FL1)
98 Y1 = Y1+TERM
99
100 PI2 = .6366198
101 Y0 = PI2*Y0
102 Y1 = -PI2/X+PI2*Y1
103
104 CHECK IF ONLY Y0 OR Y1 IS DESIRED
105
106
107 IF (N-1) 10,10,13
108 RETURN EITHER Y0 OR Y1 AS REQUIRED
109
110 IF (N) 11,12,11
111 BY = Y1
112 GO TO 19

```



```

12 BY = Y0
13 GO TO 19
14
15
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C
RHO = 1.54E6
FACTOR = 1.

C
C
READ (5,17) N,ZZ,ALPHA,A,FKHZ
READ (5,18) NPL,ANGLE
CALCULATE INITIAL VALUES
FREQ = FKHZ*1000
WRITE (6,19) N,ZZ,ALPHA,A,FKHZ,NPL,ANGLE
ALAM = 1500./FREQ
CK = 2.*PI/ALAM
Z = ALPHA
AK = CK*A
1 IF (NPL.EQ.1) GO TO 2
  PHI = 0
  NTH = 1
  GO TO 3
2 NPHI = 1
  NTH = 360
  TH = 0
3 DO 13 J=1,NPHI
  IF (NPL.EQ.1) PHI = ANGLE-1
  PHI = PHI+1
  DO 13 K=1,NTH
    L = J
    IF (NPL.EQ.1) L = K
    IF (NPL.EQ.2) TH = ANGLE-1
    IF (K.GT.180) TH = TH-1
    IF (K.LE.180) TH = TH+1
    IF (K.EQ.181) PHI = PHI+180
    APH = PHI/57.2957795
    ATH = TH/57.2957795
    ACTH = ABS(COS(ATH))
    ASTH = ABS(SIN(ATH))
    IF (ASTH.LE.0.0174525) GO TO 10
    GSUM = (0.,0.)
    SUM = (0.,0.)
  DO 9 I=1,N
    AI = I-1
    IF (AI.LT.1.) GO TO 4
    B = CMPLX(COS(AI*PI/2),-SIN(AI*PI/2))
    ASUMI = HANK(I,AK*SIN(ATH))
    IF (CABS(ASUMI).GT.(1.E+20)) GO TO 5
    SUM = (B*COS(AI*APH))/ASUMI
  C

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4 GO TO 6
  SUM = 1.0/HANK(0,AK*SIN(ATH))
5 GO TO 6
  SUM = (0.,0.)
6 ZK = CK*COS(ATH)
  GTERM = 0.
  TERM = 0.
C
  DO 8 M=1,N,2
    AL = AI
    ARG = SQRT(ZK**2+(AL**2)/(A**2))
    TERMI = 0.
    IF (M.EQ.1) TERMI = .5
    IF ((ABS(TH-90.)).LT.1.).AND.(I.EQ.1)) GO TO 7
    AR = Z*ARG
    CALL BESJ (AR,M,BJ,.1,IER)
    TERMI = BJ/AR
7 TERM = TERM+TERMI
8 GTERM = GTERM+TERM
C
  GSUM = GSUM+GTERM*SUM
9 CONTINUE
C
  GKZ = (8.0*Z*Z*GSUM)/A
  RAD(L) = (2*RHOGKZ)/(R*SIN(ATH))
  GO TO 11
10 IF (L.EQ.1) RAD(L) = (0.,0.)
  IF (L.NE.1) RAD(L) = RAD(L-1)
  GO TO 12
11 IF (KFLAG.EQ.1) RAD(L)=RAD(L)-2.*RXD(L)
12 IF (KFLAG.EQ.0) RXD(L)=RAD(L)
13 CONTINUE
C
  IF (KFLAG.EQ.0) RXD(1)=RXD(2)
  IF (KFLAG.EQ.1) RAD(1)=RAD(2)
  IF (KFLAG.EQ.1) GO TO 14
  KFLAG = 1
  ZZ = ZZ
  GO TO 1
C
14 DO 15 I=1,360
  RMAGDB(I) = 0.
  RADMAG(I) = CABS(RAD(I))
  IF (RADMAG(I).LT.1.) GO TO 15
  RMAGDB(I) = 20.*ALOG10(RADMAG(I))
15 IF (FACTOR.LT.RMAGDB(I)) FACTOR=RMAGDB(I)
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I = INT(X)
I = IABS(I)
Z = ABS(X)
IF ((Z-I).GT.0.5) I=I+1
1 IF (Z.LT.10.0) Z.GT.111.0) GO TO 2
LINE(60) = ISYM(3)
LINE(62) = ISYM(3)
K = K+1
IF (K.EQ.2) GO TO 2
I = I22-I
GO TO 1
2 LINE(61) = ISYM(2)
IF (Y.NE.0) GO TO 6
3 DO 4 K=11,111
LINE(K) = ISYM(2)
4 CONTINUE

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FILL IN GRID NUMBER LABELS ON HORIZONTAL AXIS

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IF (IPRINT.GT.1) GO TO 5
LINE(11) = ISYM(7)
LINE(20) = ISYM(10)
LINE(21) = ISYM(5)
LINE(22) = ISYM(11)
LINE(30) = ISYM(9)
LINE(31) = ISYM(5)
LINE(32) = ISYM(11)
LINE(40) = ISYM(8)
LINE(41) = ISYM(5)
LINE(42) = ISYM(11)
LINE(50) = ISYM(7)
LINE(51) = ISYM(5)
LINE(52) = ISYM(11)
LINE(61) = ISYM(7)
LINE(70) = ISYM(5)
LINE(71) = ISYM(11)
LINE(80) = ISYM(8)
LINE(81) = ISYM(5)
LINE(82) = ISYM(11)
LINE(90) = ISYM(9)
LINE(91) = ISYM(5)
LINE(92) = ISYM(11)
LINE(100) = ISYM(10)
LINE(101) = ISYM(5)

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LINE(102) = ISYM(11)
LINE(111) = ISYM(7)
GO TO 6
LINE(11) = ISYM(6)
LINE(20) = MINUS
LINE(21) = ISYM(7)
LINE(22) = ISYM(6)
LINE(30) = MINUS
LINE(31) = ISYM(8)
LINE(32) = ISYM(6)
LINE(40) = MINUS
LINE(41) = ISYM(9)
LINE(42) = ISYM(6)
LINE(50) = MINUS
LINE(51) = ISYM(10)
LINE(52) = ISYM(6)
LINE(61) = ISYM(1)
LINE(70) = MINUS
LINE(71) = ISYM(10)
LINE(72) = ISYM(6)
LINE(80) = MINUS
LINE(81) = ISYM(9)
LINE(82) = ISYM(6)
LINE(90) = MINUS
LINE(91) = ISYM(8)
LINE(92) = ISYM(6)
LINE(100) = MINUS
LINE(101) = ISYM(7)
LINE(102) = ISYM(6)
LINE(111) = ISYM(6)
CONTINUE
6 RETURN
END
SUBROUTINE NUMB (Y)
THIS SUBROUTINE PUTS DEGREE NUMBERS ON POLAR GRID
COMMON ISYM, LINE
INTEGER Y
DIMENSION ISYM(14), LINE(130)
IF (Y.NE.37) GO TO 1
LINE(33) = ISYM(7)
LINE(34) = ISYM(8)
LINE(35) = ISYM(6)
LINE(87) = ISYM(6)
LINE(88) = ISYM(12)
LINE(89) = ISYM(6)
1 IF (Y.NE.21) GO TO 2

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LINE(12) = ISYM(7)
LINE(13) = ISYM(11)
LINE(14) = ISYM(6)
LINE(108) = ISYM(6)
LINE(109) = ISYM(9)
LINE(110) = ISYM(6)
IF (Y.NE.0) GO TO 3
LINE(7) = ISYM(7)
LINE(8) = ISYM(13)
LINE(9) = ISYM(6)
LINE(113) = ISYM(6)
LINE(114) = ISYM(6)
LINE(115) = ISYM(6)
IF (Y.NE.-21) GO TO 4
LINE(12) = ISYM(7)
LINE(13) = ISYM(6)
LINE(14) = ISYM(6)
LINE(108) = ISYM(9)
LINE(109) = ISYM(9)
LINE(110) = ISYM(6)
IF (Y.NE.-37) GO TO 5
LINE(33) = ISYM(8)
LINE(34) = ISYM(10)
LINE(35) = ISYM(6)
LINE(87) = ISYM(9)
LINE(88) = ISYM(6)
LINE(89) = ISYM(6)
CONTINUE
RETURN
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END
SUBROUTINE PATCH
READ INPUT DATA IS READ FROM TWO DATA CARDS. THE FIRST CARD CONTAINS
THE SUMMING LIMIT (N), TRANSDUCER HEIGHT (ZZ) IN METERS, WIDTH (ALPHA)
IN RADIANS, RADIUS OF CYLINDRICAL Baffle (A) IN METERS, FREQUENCY
(FKHZ) IN KILOHERTZ. THE SECOND CARD CONTAINS IN PLOT INFORMAT. BOTH
FIRST ENTRY IS 'NPL'. IF NPL=1, A PLOT FOR THETA IS VARYING AS PHI.
DATA CARDS USE SAME FORMAT. COLUMNS 1-2 ARE REMAINING COLUMNS
11-20, 21-30, 31-40, 41-50 ARE F10.7. THE SECOND ENTRY ON THE
SECOND CARD IS THE VALUE (IN DEGREES) OF THE ANGLE HELD CONSTANT
COMPLEX ASUMI
COMPLEX RXDI(500)
COMPLEX SUMI
COMPLEX B, SUM, HANK, RAD(500)
DIMENSION BMAGDB(500), DATA(500), RMA3DB(500)
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C C      INITIAL VALUES
C KFLAG = 0
C R = 100
C PI = 3.1415927
C RHO = 1.54E6
C FACTOR = 1.

C C      READ (5,13) N,ZZ,ALPHA,A,FKHZ
C C      READ (5,13) NPL,ANGLE
C C      CALCULATE INITIAL VALUES
C C      WRITE (6,14) N,ZZ,ALPHA,A,FKHZ,NPL,ANGLE
C C      ALAM = 1500./FREQ
C C      CK = 2.*PI/ALAM
C C      Z = ZZ/2.
C C      AK = CK*A
C C      1 IF (NPL.EQ.1) GO TO 2
C C      NPHI = 360
C C      PHI = 0
C C      NTH = 1
C C      GO TO 3
C C      2 NPHI = 1
C C      NTH = 360
C C      TH = 0

C C      3 DO 9 J=1,NPHI
C C      IF (NPL.EQ.1) PHI = ANGLE-1
C C      PHI = PHI+1

C C      DO 9 K=1,NTH
C C      L = J
C C      IF (NPL.EQ.1) L = K
C C      IF (NPL.EQ.2) TH = ANGLE-1
C C      IF (K.GT.180) TH = TH-1
C C      IF (K.LE.180) TH = TH+1
C C      IF (K.EQ.181) PHI = PHI+180
C C      APH = PHI/57.2957795
C C      ATH = TH/57.2957795
C C      ACTH = ABS(COS(ATH))
C C      ASTH = ABS(SIN(ATH))
C C      IF (ASTH.LE.0.0174525) GO TO 6
C C      SUM = (ALPHA/PI)/HANK(0,AK*SIN(ATH))

C C      DO 4 I=1,N
C C      AI = I
C C      B = CMPLX(COS(AI*PI/2),-SIN(AI*PI/2))

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67 ASUMI = HANK(I,AK*SIN(ATH))
68 IF (CABS(ASUMI).GT.(1.E+20)) GO TO 4
69 SUM = SUM+(2*SIN(AI*ALPHA)*B*COS(AI*APH))/(AI*PI*ASUMI)
70 4 CONTINUE
71
72 IF (ACTH.LT.0.0174524) GO TO 5
73 RAD(L) = 2*RHO*SIN(CK*Z*COS(ATH))/(CK*COS(ATH)*SIN(ATH))*SUM/(R*PI
74 1)
75 RAD(L) = 2*RHO*Z*SUM/(R*PI)
76 GO TO 7
77 IF (L.EQ.1) RAD(L) = (0.,0.)
78 IF (L.NE.1) RAD(L) = RAD(L-1)
79 GO TO 8
80 IF (KFLAG.EQ.1) RAD(L)=RAD(L)-2.*RXD(L)
81 IF (KFLAG.EQ.0) RXD(L)=RAD(L)
82 9 CONTINUE
83
84 IF (KFLAG.EQ.0) RXD(1)=RXD(2)
85 IF (KFLAG.EQ.1) RAD(1)=RAD(2)
86 IF (KFLAG.EQ.1) GO TO 10
87 KFLAG = 1
88 Z = 3.*Z
89 ALPHA = 3.*ALPHA
90 GO TO 1
91
92 10 DO 11 I=1,360
93 RMAGDB(I) = 0.
94 RADMAG(I) = CABS(RAD(I))
95 IF (RADMAG(I).LT.1.) GO TO 11
96 RMAGDB(I) = 20.*ALOG10(RADMAG(I))
97 11 IF (FACTOR.LT.RMAGDB(I)) FACTOR=RMAGDB(I)
98
99 DO 12 I=1,360
100 BMAGDB(I) = RMAGDB(I)+50.-FACTOR
101 12 IF (BMAGDB(I).LT.0.) BMAGDB(I)=0.
102
103 WRITE (6,15) (I,RAD(I),RADMAG(I),RMAGDB(I),BMAGDB(I),I=1,360)
104 CALL POLPRT (1,RADMAG)
105 CALL POLPRT (2,BMAGDB)
106 RETURN
107
108 13 FORMAT (I2,8X,4F10.7)
109 14 FORMAT (T30,'NUMBER OF SUMMATIONS',T80,I5/T30,'TRANSDUCER HEIGHT(
110 1 METERS)',T80,E10.5/T30,'TRANSDUCER WIDTH(RADIANS)',T80,E10.5/
111 2T30,'RADIUS OF CYLINDER(METERS)',T80,E10.5/T30,'FREQUENCY(KHZ)',
112 3T80,E10.5/T30,'TYPE OF PLOT (1: THETA VARYING, 2: PHI VARYING)',
113 4,T80,I5/T30,'PLANE ANGLE HELD CONSTANT FOR PLOT',T80,E10.5////)
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15 FORMAT (1X,'ANGLE',19X,'RADIATION',21X,'MAGNITUDE',13X,
1,MAGN(DB),16X,'MAGN(DB)',16X,'REAL',15X,'IMAG',56X,
2,NORMALIZED',15,5E20.5))
END
SUBROUTINE PIPILOT (IYY,S)
C
C THIS SUBROUTINE SETS UP POLAR GRID INFORMATION
C
COMMON ISYM,LINE
DIMENSION LINE(130), ISYM(14), ISYN(14)
DATA ISYN/1H+,1H.,1H,1H*,1H/,1H0,1H1,1H2,1H3,1H4,1H5,1H6,1H8,1H9/
INTEGER Y,YY,W
C
C SET UP ISYM FROM ISYN FOR COMMON
C
DO 1 K=1,14
ISYM(K) = ISYN(K)
1 CONTINUE
C
C CLEAR LINE AND SET TO BLANK
C
DO 2 I=1,130
LINE(I) = ISYM(3)
2 LINE(I) = ISYM(3)
Y = 41-IYY
IF (Y.EQ.0) GO TO 7
C
C SET UP EQUATIONS FOR CONCENTRIC CIRCLES
C
YY = Y*Y
Z = (YY*2.5/2)*S
X = 61.0+SQR(2500.0-Z)
CALL LINECK (X,Y)
IF (Y.GT.32.OR.Y.LT.-32) GO TO 3
X = 61.0+SQR(1600.0-Z)
CALL LINECK (X,Y)
3 IF (Y.GT.24.OR.Y.LT.-24) GO TO 4
X = 61.0+SQR(900.0-Z)
CALL LINECK (X,Y)
4 IF (Y.GT.16.OR.Y.LT.-16) GO TO 5
X = 61.0+SQR(400.0-Z)
CALL LINECK (X,Y)
5 IF (Y.GT.8.OR.Y.LT.-8) GO TO 6
X = 61.0+SQR(100.0-Z)
CALL LINECK (X,Y)

```



```

C      SET UP EQUATIONS FOR MULTIPLES OF 30 DEGREES
6      X = 61.0+1.732051*Y*S
      CALL LINECK (X,Y)
7      X = 61.0+Y*S/1.732051
      CALL LINECK (X,Y)

C
C      PUT IN POLAR PLOT NUMBER LABELS
C
C      CALL NUMB (Y)
C      W = IABS(Y)
C
C      FILL IN POLAR PLOT AT 000, 090, 180, AND 270
C
      IF (W.NE.40) GO TO 8
      LINE(55) = I SYM(2)
      LINE(57) = I SYM(2)
      LINE(59) = I SYM(2)
      LINE(63) = I SYM(2)
      LINE(65) = I SYM(2)
      LINE(67) = I SYM(2)
      IF (W.NE.32) GO TO 9
8      LINE(56) = I SYM(2)
      LINE(58) = I SYM(2)
      LINE(60) = I SYM(2)
      LINE(62) = I SYM(2)
      LINE(64) = I SYM(2)
      LINE(66) = I SYM(2)
      IF (W.NE.24) GO TO 10
9      LINE(57) = I SYM(2)
      LINE(59) = I SYM(2)
      LINE(60) = I SYM(2)
      LINE(62) = I SYM(2)
      LINE(63) = I SYM(2)
      LINE(65) = I SYM(2)
      IF (W.NE.16) GO TO 11
10     LINE(58) = I SYM(2)
      LINE(60) = I SYM(2)
      LINE(62) = I SYM(2)
      LINE(64) = I SYM(2)
      IF (W.NE.08) GO TO 12
11     LINE(59) = I SYM(2)
      LINE(63) = I SYM(2)
12     CONTINUE
      RETURN
END
SUBROUTINE POLPRT (ITYPE,Y)
COMMON ISYM,LINE
DIMENSION NAME(80)

```



```

52 DO 10 IA=1,N
53 DATA X(IA) = Y(IA)*COS(X(IA))
54 DATA Y(IA) = Y(IA)*SIN(X(IA))
55
56
57
58
59 SORT DATA BY ORDINATE MAGNITUDE
60
61 CALL SART (DATA,X,DATA,Y,N)
62
63 DATA AND DATAY ARE SORTED BY DESCENDING MAGNITUDE ON THE DATAY VAL
64 SET UP FOR PLOTTING POLAR GRID WITH DATA
65
66
67
68
69 DO 6 IYY=1,81
70
71 CALL PTPLOT (IYY,S)
72
73 LINE IS RETURNED WITH POLAR GRID INFORMATION
74
75 SET UP 'Y' BIN SIZE UPPER AND LOWER LIMITS
76 ULL IS THE LOWER BIN LIMIT
77 UL IS THE UPPER BIN LIMIT
78
79 BIN = DIM/80.0
80 ULL = DIM-(2*IYY-1)*BIN
81 UL = ULL+2*BIN
82
83
84 CYCLE THROUGH DATA TO FIND WHICH ONES FALL IN 'Y' BINS
85
86
87 IF (NST.GT.N) GO TO 5
88
89
90 DO 4 JJ=NST,N
91 IF (DATAY(JJ).LT.ULL) GO TO 5
92 KST = JJ
93 AMAG = SQRT((DATA(X(JJ)*DATA(X(JJ))+DATAY(JJ)*DATAY(JJ))
94
95 CHECK THAT MAGNITUDE IS NOT OVER DIM
96
97 IF (AMAG.GT.DIM) GO TO 4
98
99 OK IS THE FINAL LINE POSITION FOR THE '**

```


C	OK = DATA(JJ)*S*40.0/DIM+61.0	100
	IF (OK.LT.10.0) GO TO 4	101
	K = INT(OK)	102
	K = IABS(K)	103
	OK = ABS(OK)	104
	IF ((OK-K).GT.0.5) K=K+1	105
	IF (OK.LT.10.0.OR.OK.GT.111.0) GO TO 4	106
	LINE(K) = ISYM(4)	107
C	4 CONTINUE	108
C	5 CONTINUE	109
	NST = KST+1	110
C	PRINT OUT ONE LINE OF PLOT	111
C	WRITE (6,9) LINE	112
C	6 CONTINUE	113
C	RETURN	114
C	7 FORMAT(1H1,' NORMALIZED MAGNITUDE PATTERN',T90,'NORMALIZING FACTOR	115
	1=E12.5)	116
	8 FORMAT(1H1,' NORMALIZED DECIBEL(DB) PATTERN',T90,'NORMALIZING	117
	1FACTOR=E12.5)	118
	9 FORMAT(1X,130A1)	119
	END	120
	SUBROUTINE SORT (DATA,DATA,N)	121
	DIMENSION DATA(500), DATA(500)	122
	THIS ROUTINE SORTS DATA IN DATA BY MAGNITUDE	123
C	NN = N-1	124
C	DO 2 I=1,NN	125
C	NM = I+1	126
	DO 1 J=NM,N	127
	IF (DATA(I).GE.DATA(J)) GO TO 1	128
	STOR = DATA(I)	129
	DATA Y(I) = DATA(J)	1
	DATA Y(J) = STOR	2
	STOR = DATA(I)	3
	DATA X(I) = DATA(J)	4
	DATA X(J) = STOR	5
C		6
		7
		8
		9
		10
		11
		12
		13
		14
		15
		16
		17
		18


```

19 1 CONTINUE
20 2 CONTINUE
21
22 RETURN
23
24 SUBROUTINE SEG
1 2 READ INPUT DATA
3 3 THE INPUT DATA IS READ FROM TWO DATA CARDS. THE FIRST CARD CONTAINS
4 4 THE SUMMING, LIMIT OF CYLINDRICAL BAFFLE (ZZ) IN METERS, WIDTH (ALPHA)
5 5 IN RADIANS, RADIUS OF CYLINDRICAL BAFFLE (A) IN METERS, FREQUENCY
6 6 (FKHZ) IN KILOHERTZ. THE SECOND CARD CONTAINS THETA VARYING AS PHI
7 7 (FIRST ENTRY IS 'NPL'. IF NPL=1, A PLOT FOR THETA IS REMAINING ON THE
8 8 IS HELD CONSTANT, NPL=2, PHI VARIES AND THE SECOND ENTRY ON THE
9 9 DATA CARDS USE SAME FORMAT. COLUMNS 1-2 ARE I2. REMAINING COLUMNS
10 10 11-20, 21-30, 31-40, 41-50 ARE F10.7. THE SECOND ENTRY ON THE
11 11 SECOND CARD IS THE VALUE (IN DEGREES) OF THE ANGLE HELD CONSTANT
12 12 EITHER A '1' OR '2' IN COLUMN 2 OF THE THIRD DATA CARD.
13 13 IF NO SHADING PATTERN IS DESIRED, THE 3RD DATA CARD IS LEFT BLANK.
14 14 IF THE 3RD DATA CARD CONTAINS A '1' OR A '2', THE FOURTH(4) AND
15 15 SUCCEEDING DATA CARDS WILL CONTAIN THE AMPLITUDE AND FOURTH DATA
16 16 SHADING INFORMATION. TO ENTER THIS INFORMATION, TO BE SHADED
17 17 CARD MUST CONTAIN THE TOTAL NUMBER OF ELEMENTS, 1-3, FOR FIVE
18 18 (MAXIMUM OF 120 ELEMENTS) IN COLUMNS 1-3. THAT IS, FOR FIVE
19 19 ELEMENTS A '5' IN COLUMN 3. A SEPARATE DATA CARD FOR EACH OF THE
20 20 COLUMNS '2' AND '3'. A SEPARATE DATA CARD FOR EACH OF THE DATA CARD
21 21 ELEMENTS, FOR THE TOTAL NUMBER OF ELEMENTS SPECIFIED ON DATA CARD
22 22 FOUR(4) IS THEN ENTERED CONSECUTIVELY IN THE FOLLOWING FORMAT:
23 23 COLUMNS 1-3, SPECIFIES ELEMENT NUMBER, COLUMNS 11-20 IN F10.5
24 24 FORMAT) SPECIFIES THE AMPLITUDE SHADING, AND COLUMNS 21-30 IN
25 25 F10.5 FORMAT) SPECIFIES PHASE SHADING ENTERED AS AN ANGLE
26 26 (EXAMPLE, ASUMI
27 27 COMPLEX SUMI
28 28 COMPLEX SUMI
29 29 DIMENSION AMP(500)
30 30 DIMENSION BMAGDB(500)
31 31 COMPLEX TERM(50)
32 32 COMPLEX CORP
33 33 COMPLEX AASS
34 34 DIMENSION AMP(120), SHADE(120), ASHAD(120), ARRAD(500)
35 35 DIMENSION BMAGDB(500)
36 36 COMPLEX RRAD(500)
37 37 COMPLEX B, SUM, HANK, RAD(500)
38 38 DIMENSION RADMAG(500), DATA(500), RMAGDB(500)
39 39
40 40 INITIAL VALUES
41 41 R = 100.
42

```



```

43 PI = 3.1415927
44 RHO = 1.54E6
45 FACTOR = 1.
46 BOSS = 1.
47
48
49
50 READ (5,20) N,ZZ,ALPHA,A,FKHZ
51 READ (5,20) NPL,ANGLE
52 CALCULATE INITIAL VALUES
53 FREQ = FKHZ*1000.
54 WRITE (6,21) N,ZZ,ALPHA,A,FKHZ,NPL,ANGLE
55 ALAM = 1500./FREQ
56 CK = 2.*PI/ALAM
57 Z = ZZ/2.
58 AK = CK*A
59 IF (NPL.EQ.1) GO TO 1
60 NPHI = 360
61 PHI = 0
62 NTH = 1
63 GO TO 2
64
65 1 NPHI = 1
66 NTH = 360
67 TH = 0
68
69
70
71
72
73
74
75
76
77
78
79
80
81
82
83
84
85
86
87
88
89
90

```



```

91 ASUMI = HANK(I,AK*SIN(ATH))
92 IF (CABS(ASUMI).GT.(1.E+20)) GO TO 3
93 SUM = SUM+(2*SIN(AI*ALPHA)*B*COS(AI*APH))/(AI*PI*ASUMI)
94 3 CONTINUE
95
96
97 IF (ACTH.LT.0.0174524) GO TO 5
98 RAD(L) = 2*RHO*SIN(CK*Z*COS(ATH))/(CK*COS(ATH)*SIN(ATH))*SUM/(R*PI
99 1)
100 GO TO 6
101 IF (L.EQ.1) RAD(L) = (0.,0.)
102 IF (L.NE.1) RAD(L) = RAD(L-1)
103 GO TO 6
104 5 RAD(L) = 2*RHO*Z*SUM/(R*PI)
105 6 CONTINUE
106
107 RAD(1) = RAD(2)
108
109 DO 7 I=1,360
110 RMAGDB(I) = 0.
111 RADMAG(I) = CABS(RAD(I))
112 IF (RADMAG(I).LT.1.) GO TO 7
113 RMAGDB(I) = 20.*ALOG10(RADMAG(I))
114 7 IF (FACTOR.LT.RMAGDB(I)) FACTOR=RMAGDB(I)
115
116
117 DO 8 I=1,360
118 BMAGDB(I) = RMAGDB(I)+50.-FACTOR
119 8 IF (BMAGDB(I).LT.0.) BMAGDB(I)=0.
120
121 WRITE (6,22) (I,RAD(I),RADMAG(I),RMAGDB(I),BMAGDB(I),I=1,360)
122 CALL POLPRT (1,RADMAG)
123 CALL POLPRT (2,BMAGDB)
124 READ (5,20) NPL
125 IF (NPL.EQ.0) RETURN
126 READ (5,19) NUMB
127
128 DO 9 I=1,120
129 AMP(I) = 0.
130 9 SHADE(I) = 0.
131
132 DO 10 I=1,NUMB
133
134
135
136
137
138

```



```

139 READ (5,19) L,X,Y
140 AMP(L) = X
141 SHADE(L) = Y
142
143 WRITE (6,23)
144 WRITE (6,24) (I,AMP(I),SHADE(I),I=1,120)
145
146 DO 11 I=1,120
147   11 ASHAD(I) = SHADE(I)/57.2957795
148
149 DO 12 I=1,360
150   12 RRAD(I) = (0.,0.)
151
152 DO 14 I=1,N
153   AI = I-1
154   IF (AI.EQ.0.) GO TO 13
155   B = CMPLX(COS(AI*PI/2),-SIN(AI*PI/2))
156   TERM(I) = (2*SIN(AI*ALPHA)*B)/(AI*PI*HANK(I,AK))
157   GO TO 14
158   13 TERM(I) = (ALPHA/PI)/HANK(0,AK)
159   14 CONTINUE
160
161 CONS = (2*RHO*Z)/(R*PI)
162 PHI = 0
163
164 DO 16 M=1,360
165   DO 16 K=1,120
166     PHI = (K-1)*3.141592653589793/120
167     AAPHI = PHI/57.2957795
168     AASS = CMPLX(COS(ASHAD(K)),SIN(ASHAD(K)))
169     SUM = (0.,0.)
170
171 DO 15 J=1,N
172   AJ = J-1
173   SUM = SUM+(TERM(J))*(COS(AJ*AAPHI))
174
175
176
177
178
179
180
181
182
183
184
185
186

```



```

C      RRAD(M) = AMP(K)*AASS*SUM*CONS+RRAD(M)
16 CONTINUE
C
C
C
C      DO 17 I=1,360
ARRDB(I) = 0
ARRAD(I) = (CABS(RRAD(I)))
IF (ARRAD(I).LT.1.) GO TO 17
ARRDB(I) = 20*ALOG10(ARRAD(I))
17 IF (BOSS.LT.ARRDB(I)) BOSS=ARRDB(I)
C
C
C
C      DO 18 I=1,360
ARRDB(I) = ARRDB(I)+50.-BOSS
18 IF (ARRDB(I).LT.0.) ARRDB(I)=0.
C
C
C      WRITE (6,25) (I,RRAD(I),ARRAD(I),ARRDB(I),I=1,360)
CALL POLPRT (1,ARRAD)
CALL POLPRT (2,ARRDB)
RETURN
C
C
19 FORMAT (I3,7X,2F10.5)
20 FORMAT (I2,8X,4F10.7)
21 METERS),T80,E10.5/T30,TRANSUCER HEIGHT(
2130,RADIUS OF CYLINDER (METERS),T80,E10.5/T30,FREQUENCY(KHZ),
3T80,E10.5/T30,TYPE OF PLOT (1: HETA VARYING, 2: PHI VARYING),
4,T80,I5/T30,PLANE ANGLE HELD CONSTANT FOR PLOT,T80,E10.5///)
22 ,MAGN(DB),16X,REAL,15X,IMAG,56X,
2 ,NORMALIZED/(I5,5E20.5))
23 FORMAT (4(IX,13,6X,2X,AMPLITUDE,2X,PHASE,4X))
24 14X,F6.1,7X,13,6X,F4.1,4X,F6.1,7X,I3,6X,F4.1,
25 1X,ANGLE,19X,RADIATION,21X,MAGNITUDE,13X,
1,MAGN(DB),16X,REAL,15X,IMAG,44X,NORMALIZED/(I5,4E20.5)
END
230

```


APPENDIX B

MAIN

Purpose: To control program

Method: The program inspects the first four (4) letters of the coded titles (DISK, PATCH, SEGEMENT - Note the spelling of the "Segment" design) to transfer control to the proper subroutine. It also writes out the first line of output identifying the design configuration being calculated.

Called By: First Input Data Card

Calls To: DISK
PATCH
SEG

HANK

Purpose: To calculate a Hankel derivative given the order and argument.

Method: This subroutine is a function subroutine which calculates the Hankel derivative by the recurrence relation, $H'_{(M)}(R) = \frac{M}{R} H_{(M)}(R) - H_{(M+1)}(R)$. The Hankel function of order (M) and order (M+1) are calculated by combining the "J" and "Y" Bessel functions as a complex number.

Called By: DISK
PATCH
SEGMENT

Calls To: BESY
BESJ

DISK

Purpose: To calculate the radiation pattern for the "Disk" design.

Method: The "DO" loop ending with statement number nine (9) calculates the pattern for the "DISK" design. It contains within it, a second "DO" loop ["DO loop ending with statement number eight (8)] which calculates the infinite series composed of the odd Bessel Functions. The entire loop is executed two times through the use of the indicator, "KFLAG." After the second execution of the loop, twice the results of the first execution are subtracted from those of the second execution. The statement, "IF(KFLAG.EQ.1) GO TO 14" transfers the results of the calculations to the plotting package.

Called By: MAIN

Calls To: HANK
POLPRT

PATCH

Purpose: To calculate the radiation pattern for the "Patch" design.

Method: The basic equations derived for the "Patch" design are coded in the "DO" loop ending with statement number nine (9). The pattern is achieved by executing that "DO" loop twice. In the first execution of the loop, the pattern for the oppositely phase shaded center element is calculated. Subsequently, "KFLAG" (an indicator of how many times the

loop has been executed) is updated, and the dimensions of the element changed to those of the outer (larger) element. After the second execution of the loop, two (2) times the first pattern is subtracted from the pattern obtained during the second execution of the loop. The "IF" statement, IF(KFLAG.EQ.1) GO TO 10" transfers the calculations to the plotting subroutines.

Called By: MAIN

Calls To: HANK
POLPRT

SEG

Purpose: To calculate the radiation pattern for the "Segment" design.

Method: This subroutine can be thought to consist of two parts. All statements previous to the statement, "READ (5,17) NPL" are involved in computing the pattern for a single element, while all statements after that statement calculate the pattern for the array (horizontal plane only, i.e. $\theta = 90$ degrees) with amplitude and phase shading incorporated.

Dependent on the initial "NPL" code, the "DO" loop ending with statement number six (6) varies either angle θ or angle ϕ in one (1) degree increments.

The angle held constant (second entry on the third card of the input data deck) in consonance with the angle to be varied (dictated by the "NPL" code) specifies the plane in which the pattern is determined.

In the second part of the subroutine (amplitude and phase shading), the "DO" loop ending with statement number sixteen (16) is the coded version of the general expression for the amplitude and phase shading derived earlier for the horizontal plane.

Called By: MAIN

Calls To: HANK
POLPRT

POLPRT

Purpose: To control the plotting of the polar plot.

Method: This subroutine is the main subroutine in the polar plot package and is responsible for calling the various subroutines of the package.

The scale factor, S, must be changed according to the printer characteristics. The scale factor in this subroutine is set for ten, 10, characters per inch for the abscissa and eight, 8, characters per inch for the ordinate axis. Therefore $S = 10./8$.

After initializing DATAX, DATAY, and X, the input data, Y, is scanned to determine the normalizing factor. If this normalizing factor is less than 1.E-32, an error statement is printed and the plotting is aborted.

In the DO LOOP ending with statement 8, each line of the polar plot is printed after a call is made to PTPLLOT to establish the polar grid information. The variable, DIM,

is used as a scaling factor for the polar plot. The value of 1.0 will cause all of input data to be plotted, however, if only the values less than one-half of the normalizing factor are of interest, then DIM can be set to .5. This will enlarge the center of the polar plot.

Called By: SEG
PATCH
DISK

Calls To: PTPLOT
SART

PTPLOT

Purpose: To establish the grid information for the polar plot.

Method: In the DO LOOP ending at statement 1 the alphanumeric characters are transferred to ISYN in order to pass via COMMON to other subroutines. In the statements following statement 2, the equations for the plotted concentric circles are established. Below statement 7 the grid marks on the 090-270 axis are inserted.

Called By: POLPRT

Calls To: LINECK
NUMB

NUMB

Purpose: To place degree numbers on the polar plot.

Method: The current line which is being printed is passed to the subroutine in the calling argument. If this line contains degree numbers, these numbers are placed in the correct position by the IF statements.

Called By: PTPLOT

Calls To: NONE

LINECK

Purpose: To insert grid characters on the polar plot.

Method: The period character (ISM(2)) is inserted in the proper position in the statements above statement 4. In the statements after statement 4, the grid numbers labels are inserted on the horizontal axis.

Called By: POLPLOT

Calls To: NONE

APPENDIX C

SEGEMENT 20 1	.02 0.	.0187479	.2667	75.
SEGEMENT 20 2 2 7	.02 90.	.0187479	.2667	75.
118	1.	0.		
119	.8	0.		
120	.3	0.		
1	.1	0.		
2	.3	0.		
3	.8	0.		
4	1.	0.		
PATCH 20 1	.02 0.	.0187479	.2667	75.
PATCH 20 2	.02 90.	.0187479	.2667	75.
DISK 20 1	.025 0.	.0135	.2667	75.
DISK 20 2	.025 90.	.0135	.2667	75.

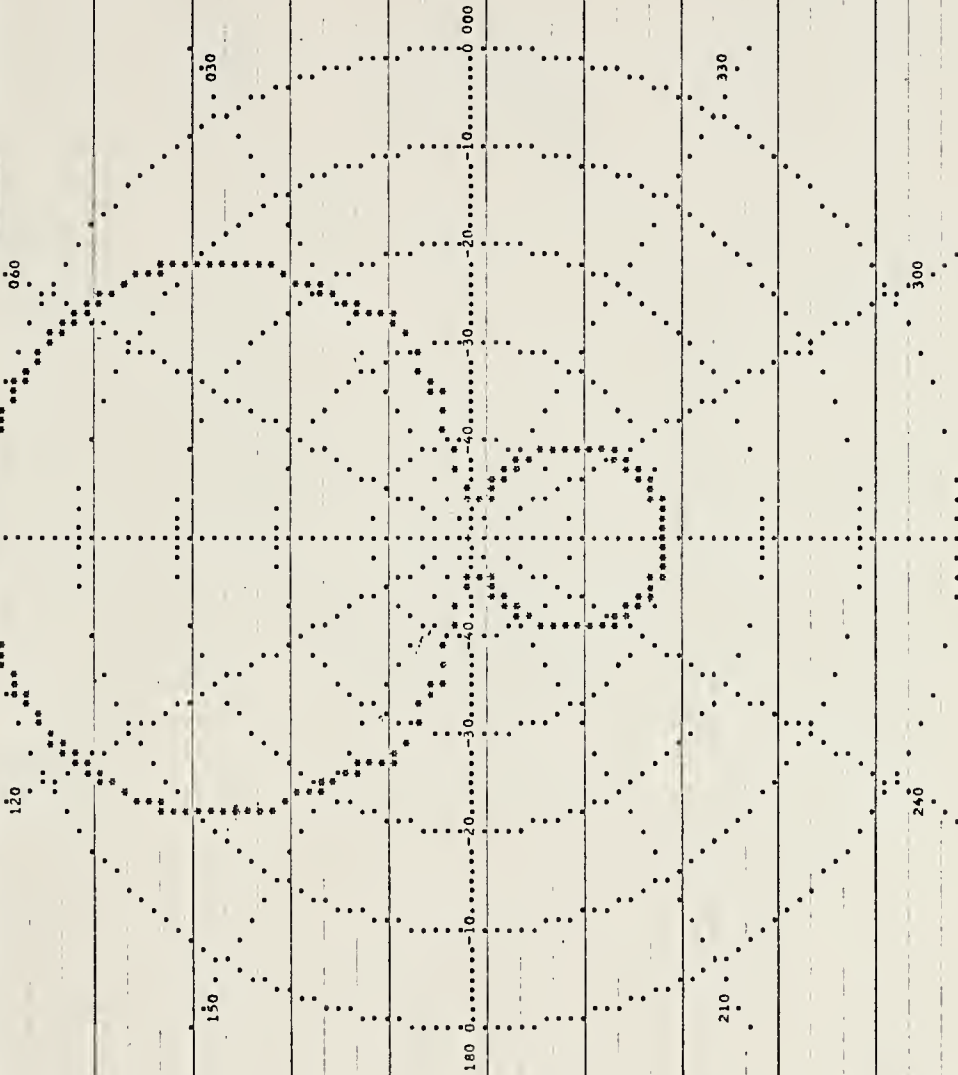
APPENDIX D

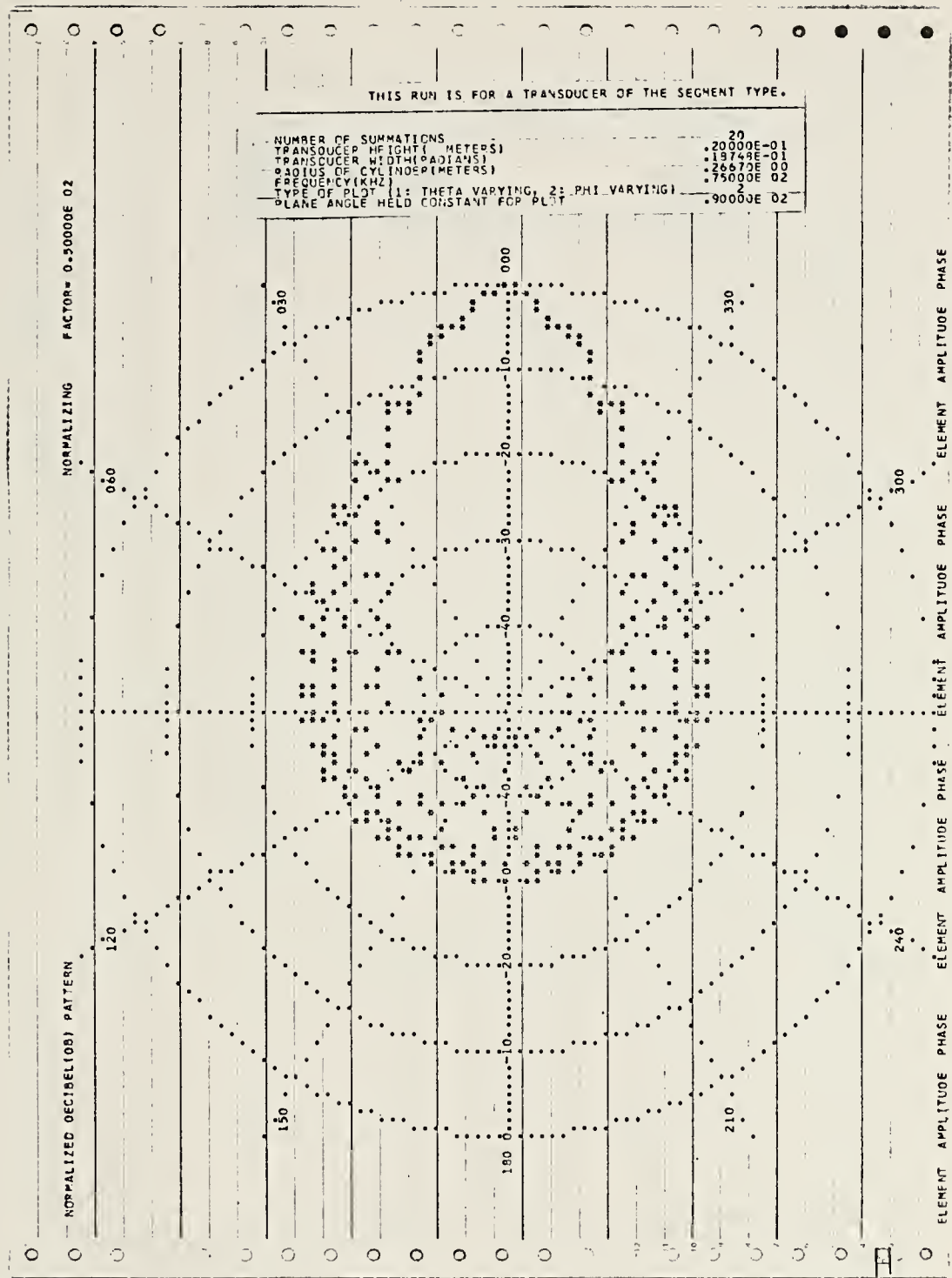
THIS RUN IS FOR A TRANSDUCER OF THE SEGMENT TYPE.

NUMBER OF SUMMATIONS 20
 TRANSDUCER HEIGHT (METERS) .20000E-01
 TRANSDUCER WIDTH (RADIAN) .18748E-01
 RADIUS OF CYLINDER (METERS) .25670E-00
 FREQUENCY (KHZ) .75000E-02
 TYPE OF PLOT (1: THETA VARYING, 2: PHI VARYING) 1
 PLANE ANGLE HELD CONSTANT FOR PLOT .0

NORMALIZING FACTOR = 0.50000E 02

NORMALIZED DECIBEL (DB) PATTERN





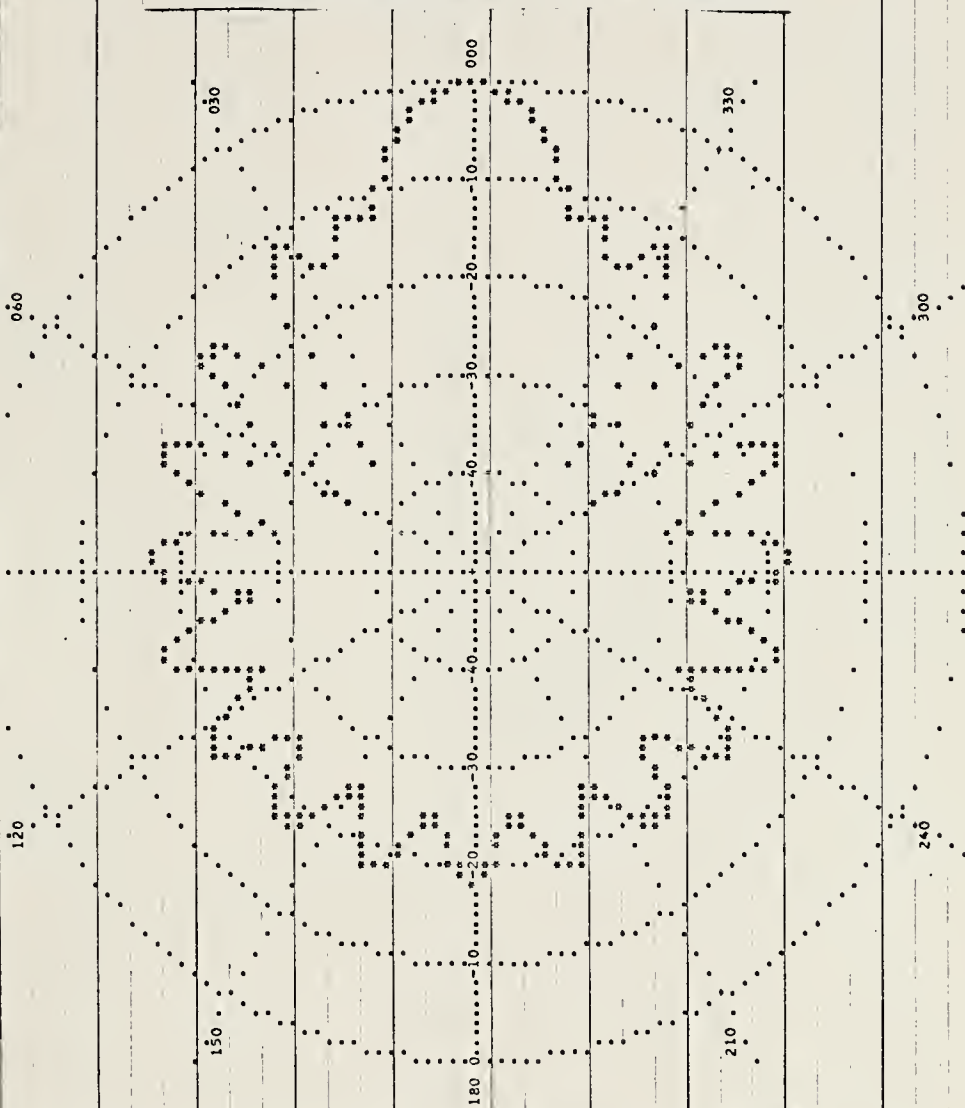
THIS RUN IS FOR A TRANSDUCER OF THE SEGMENT TYPE.

NUMBER OF SUMMATIONS	20
TRANSDUCER HEIGHT (METERS)	.20000E-01
TRANSDUCER WIDTH (RADIANS)	.19749E-01
RADIUS OF CYLINDER (METERS)	.26670E-00
FREQUENCY (KHZ)	.75000E-02
TYPE OF PLOT (1: THETA VARYING, 2: PHI VARYING)	2
PLANE ANGLE HELD CONSTANT FOR PLOT	.90000E-02

NORMALIZING FACTOR = 0.50000E-02

NORMALIZED DECIBEL (OR) PATTERN

NORMALIZED DECIBEL (OR) PATTERN



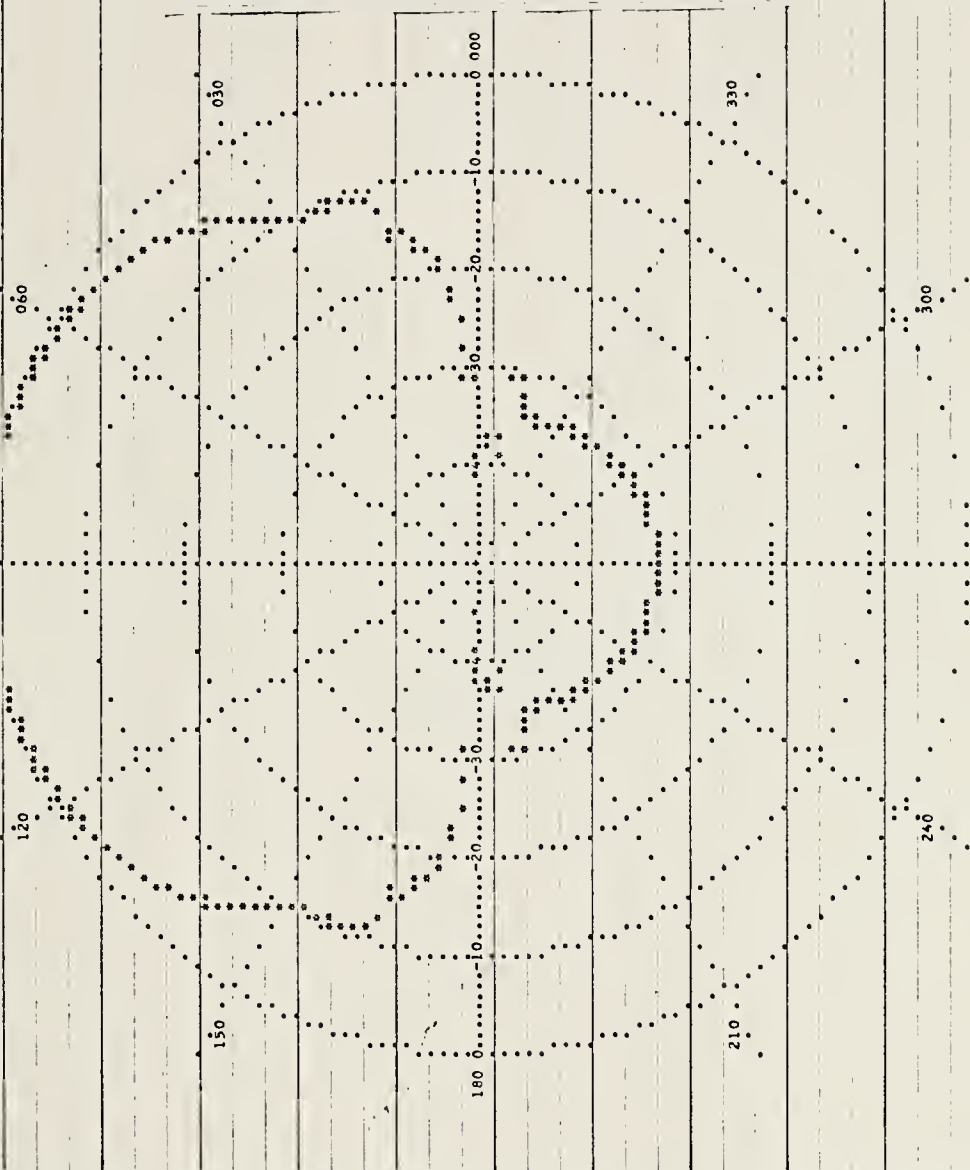
SEVEN (7) ELEMENTS SHADED AS PER APPENDIX C

THIS RUN IS FOR A TRANSDUCER OF THE PATCH TYPE.

NUMBER OF SUMMATIONS 20
 TRANSDUCER HEIGHT (METERS) .20000E-01
 TRANSDUCER WIDTH (RADIAN) .18749E-01
 RADIUS OF CYLINDER (METERS) .26670E+00
 FREQUENCY (KHZ) .75000E+02
 TYPE OF PLOT (1: THETA VARYING, 2: PHI VARYING) 1
 PLANE ANGLE HELD CONSTANT FOR PLOT .0

NORMALIZING FACTOR= 0.50000E 02

NORMALIZED DECIBEL (DB) PATTERN



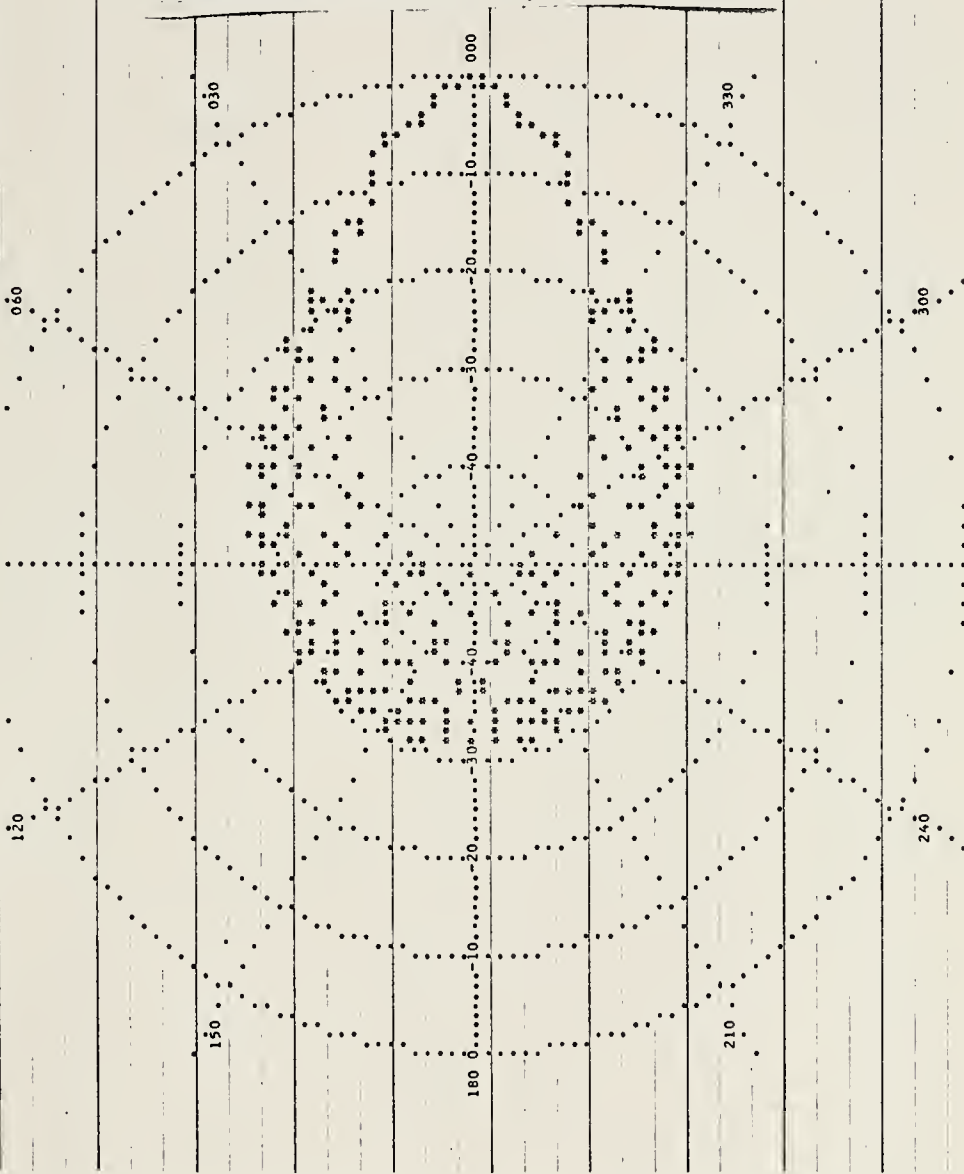
NORMALIZED DECIBEL(DB) PATTERN

NORMALIZING

FACTOR= 0.50000E 02

THIS RUN IS FOR A TRANSDUCER OF THE PATCH TYPE.

NUMBER OF SUMMATIONS	20
TRANSDUCER HEIGHT (METERS)	.20000E-01
TRANSDUCER WIDTH (RADIANS)	.18748E-01
RADIUS OF CYLINDER (METERS)	.28670E 00
FREQUENCY (KHZ)	.75000E 02
TYPE OF PLOT (1: THETA VARYING, 2: PHI VARYING)	2
PLANE ANGLE HELD CONSTANT FOR PLOT	.90000E 02

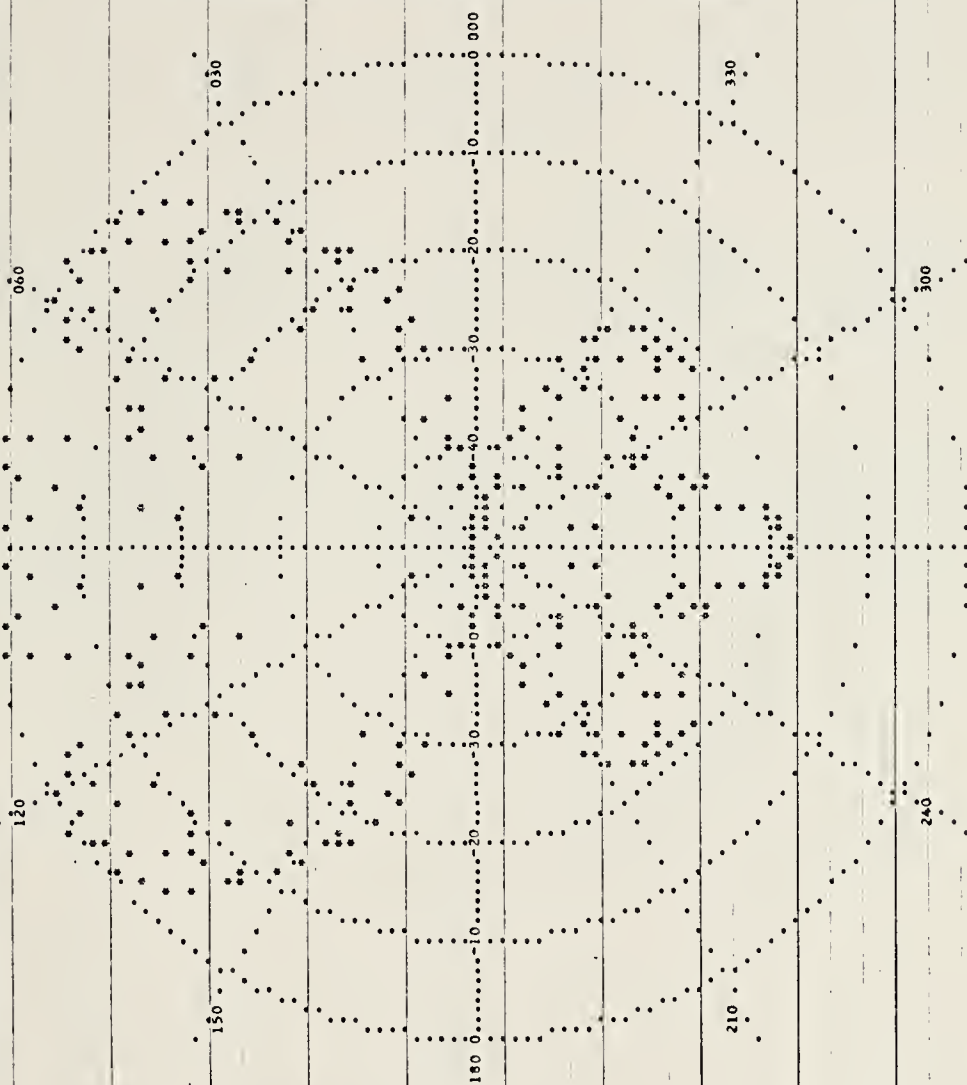


THIS RUN IS FOR A TRANSDUCER OF THE DISK TYPE.

NUMBER OF SUMMATIONS 20
 OUTER RADIUS OF DISK(METERS) .25000E-01
 INNER RADIUS OF DISK(METERS) .13500E-01
 RADIUS OF CYLINDER(METERS) .25670E-00
 FREQUENCY(K-HZ) .75000E-02
 TYPE OF PLOT (1: THETA VARYING, 2: PHI VARYING) 1
 PLANE ANGLE HELD CONSTANT FOR PLOT .0

NORMALIZING FACTOR= 0.50000E 02

NORMALIZED DECIBEL(08) PATTERN

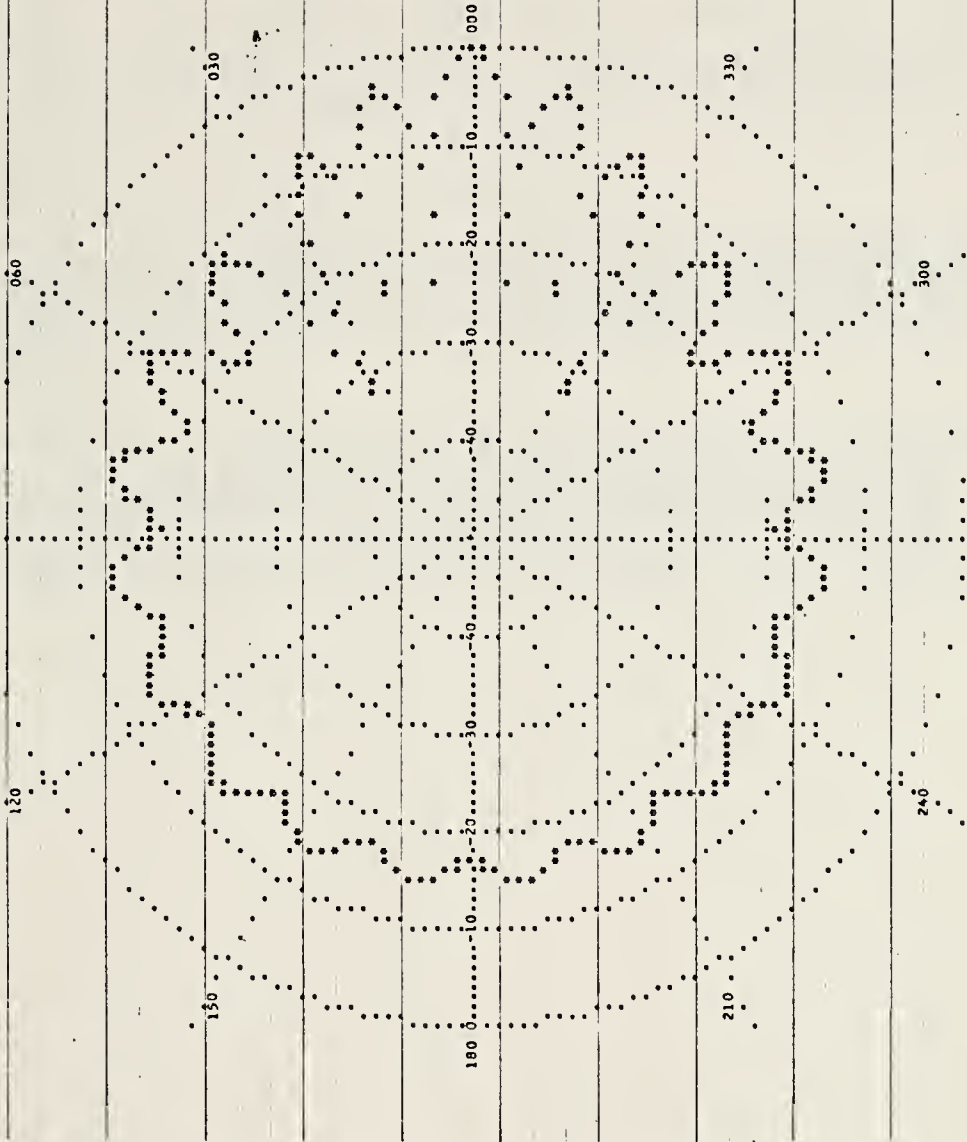


THIS RUN IS FOR A TRANSJECER OF THE DISK TYPE.

NUMBER OF SUMMATIONS 20
 OUTER RADIUS OF DISK (METERS) .25000E-01
 INNER RADIUS OF DISK (METERS) .13500E-01
 RADIUS OF CYLINDER (METERS) .76670E-03
 FREQUENCY (KHZ) .75000E-02
 TYPE OF PLOT (1: THETA-VARYING, 2: PHI VARYING) 2
 PLANE ANGLE HELD CONSTANT FOR PLOT .90000E-02

NORMALIZING FACTOR= 0.50000E 02

NORMALIZED DECIBEL (DB) PATTERN



LIST OF REFERENCES

1. Laird, D.T. and Cohen, H., "Directionality Patterns for Acoustic Radiation from a Source on a Rigid Cylinder," The Journal of the Acoustical Society of America, v. 24(1), p. 46-49, January 1952.
2. Morse, P.M., Vibration and Sound, McGraw-Hill, 1948.
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